## The Bias of the ECB Inflation Projections: a State Dependent Analysis

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- Accuracy of published forecasts deteriorated during the financial crisis and the COVID-19 pandemic (NY FED: Potter 2012, ECB and NY FED: Alessi, Ghysel Onorante Peach and Potter 2014, MPC BoE: Stockton 2012, BoE DSGE: Fawcett, Koerber Masolo and Waldron 2015)
- Following the 2007-2008 financial crisis many monetary authorities consistently overestimated inflation (Riksbank: Iversen Laseen Lundvall and Soderstrom 2016, ECB: Kontogeorgos and Lambrias 2019)
- During the pandemic reopening central banks consistently underestimated inflation (ECB: Economic Bullettin 3/2022) COVID
- Repeated large and systematic projection errors may:
  - increase the risk of deanchoring of inflation expectations

deteriorate the credibility of the monetary authority

## ECB Projections 1999Q1-2021Q4



Figure: Actual year-over -year Harmonized Index of Consumer Prices Inflation (HICP), solid blue line with marker, and ECB Quarterly Projections for 1999Q1-2021Q4, grey lines. Projections are produced for the current and following two calendar years, i.e. up to eleven quarters ahead in Q1 and for at most eight quarters ahead in Q4.

## ECB Inflation Projections



Figure: ECB Projections for HICP Inflation 1999Q1-2021Q4. Shaded areas mark the maximum (blue) and minimum (red) projections,  $10^{th}$  and  $25^{th}$  ( $75^{th}$  and  $90^{th}$ ) percentiles and the medians (solid lines) conditional on whether inflation was above or below 1.8% (green dotted line) during each projection exercise.

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## Testing for Bias

Forecast Error:

$$Error_{t,h} = y_{t+h} - y_{t+h|t} = \epsilon_{t,h} \tag{1}$$

Linear Model (Holden and Peel, 1990):

$$\epsilon_{t,h} = \mu_h + u_{t+h|t} \qquad (2)$$

Null hypothesis of no bias:  $\mu_h = 0$ .

Overall, does the ECB systematically under(over) predict inflation?

State Dependent Model(Odendhal, Rossi and Sekhposyan, 2022):

$$\epsilon_{t,h} = \mu_h + \theta_h G\left(S_t; \gamma_h\right) + u_{t+h|t} \tag{3}$$

We assume G (S<sub>t</sub>; γ<sub>h</sub>) is a threshold regression model:

$$G\left(S_t;\gamma_h\right) = \mathbb{1}\left(S_t \ge \gamma_h\right). \tag{4}$$

i.e. expected value of  $\epsilon_{t,h}$  might differ according on whether  $S_t$  is above or below the unknown threshold  $\gamma_h$ . This state dependent model leads to:

$$E\left(\epsilon_{t,h}\right) = \begin{cases} \mu_h & \text{if } S_t < \gamma_h\\ \mu_h + \theta_h & \text{if } S_t \ge \gamma_h \end{cases}$$

▶ Does ECB systematically under(over) predict inflation when inflation is above/below a certain value? ▶ previous studies

## Implementation

- Dataset: Quarterly Eurosystem/ECB staff projections for yoy overall HICP inflation over 1999Q1-2021Q4 from nowcasting till 8 quarters ahead
  - ▶ 92 (84) observations for nowcasting (eight quarters ahead)
  - ECB staff (March and September), ECB staff + experts in national central banks (June and December)
  - monthly inflation projections are provided by national central bank experts for up to 11 months (NIPE).
  - external assumptions, combination of models, expert knowledge, judgement
  - forecasts evaluated against latest available vintage (2022Q1) as revisions for inflation series negligible



- approximate the information set available to the staff at the time of forecasting
- cutoff dates approximately between week 6 and 8 of the quarter
- ► ECB observes: previous quarter yoy inflation rate  $(\pi_{t-1}^Q)$ , first month yoy inflation of current quarter  $(\pi_t^{M1})$

•  $S_t = \left(\pi_{t-1}^Q + \pi_t^{M\,1}\right)/2$ 

## Bias in ECB Inflation Projections



Figure: Estimated bias in ECB Projections for HICP Inflation 1999Q1-2021Q4. Ctable

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## Bias Results: Discussion

No bias in the linear model

Evidence of bias in the state dependent model:

 ECB systematically overpredicts (underpredicts) inflation when inflation is below (above) the target

negative and positive errors cancel out so no bias on average

Bias is larger in absolute value when inflation is above target

•  $\mu$  average of -0.05 when  $S_t < \gamma$ 

•  $\mu + \theta$  average of 0.23 when  $S_t \ge \gamma$ 

Evidence of bias stronger at the medium horizon

- bias is larger for intermediate horizons 3, 4, 5
- $\mu + \theta$  average of 0.36 over h = 3, 4, 5 surveys
- Threshold value  $\gamma$  consistent with ECB implicit target estimated by Hartmann and Smets (2018), Rostagno et al. (2019) threshold

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## Bias in the Literature

- No Bias: Greenbook (Clements et al. 2007); FOMC 2009-2015 (Arai 2016); Greenbook over 1986-2006 (El Shagi et al. 2016); Greenbook overall and conditioning on recession (Messina et al. 2015), Kontogeorgeos and Lambrias (2019)
- Bias: Greenbook, underprediction till 1975, overprediction after 1979 (Capistran 2008); Greenbook over recessions and/or inflation cycles Sinclair et al. (2010); Greenbook over rolling samples El Shagi et al. (2016); positive bias of BMPE forecasts (Fisher et al. 2009); six small open economies 2000-2013 (Gomez-Barrero and Parra-Polania 2014); 12-24 months forecasts of core from 10 small open economies (Charemza and Ladley 2016); Kontogeorgeos and Lambrias (2019) for intermediate horizons under prediction in early part of the sample, over-prediction during 2010-2013
- Biased forecast not necessarily irrational. Theoretical models attribute empirical bias to:
  - asymmetric loss function: Capistran (2008)
  - strategic communication: Gomez-Barrero and Parra-Polania (2014)
  - heterogeneous agents beliefs: Herbert (2020)
  - distortion from MPC voting system: Charemza and Ladley (2016)

## Bias: The Role of External Assumptions

- ECB/Eurosystem projections rely on set of assumptions on economic environment:
  - short term interest rates (3month Euribor): market expectations derived from futures rates
  - exchange rates (EUR/USD): random walk, average over previous two weeks
  - ▶ oil prices: average futures price of Brent crude oil over previous two weeks
- Exogenous conditioning assumptions, not affected by ECB inflation projections published in the same quarter
- Can errors in the exogenous variables drive the errors in inflation forecasts?
- Test whether bias still present after controlling for the errors in the external assumptions

$$\epsilon_{t,h} = \mu_{1,h} + \mu_{2,h}\zeta_{t,h} + \theta_h G\left(S_t;\gamma_h\right) + u_{t+h|t} \tag{5}$$

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with  $\zeta_{t,h}^i=z_t^i-z_{t|t-h}^i$  and  $z_t^i$  the realization and  $z_{t|t-h}^i$  exogenous assumption

 Rationale: if systematic errors in the external assumptions were driving the forecast errors, then the nonlinear term should not have additional explanatory power. <a href="https://bias.in.external">bias.in.external</a>

## Bias in ECB Inflation Projections



Figure: Estimated bias in ECB Projections for HICP Inflation after controlling for errors in the external assumptions, 1999Q1-2021Q4. ( table

Bias and Exogenous Assumptions Results: Discussion

• Evidence of state dependent bias after controlling for the errors in exogenous assumptions:

- magnitude unaffected
- significance unaltered
- When conditioning on interest rates:
  - significance of non-linear term for all horizons except nowcast
  - interest rates errors significant only for h = 2
- ▶ When conditioning on exchange rate:
  - ▶ significance of non-linear term at short and intermediate horizons for h = 1 4 and pooled

- exchange rates errors significant only when all horizons are pooled
- When conditioning on oil prices:
  - ▶ significance of non-linear term from h=2, and pooled
  - errors in oil prices significant in the short horizons h = 0 3

## Robustness Analysis

Results are robust to:

 alternative assumptions on the information set available to the ECB at the time of forecasting: ( infoset )

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- nowcast
- actual inflation
- first month only
- last three months
- using a known threshold,  $\gamma \leq 1.8$  known gamma
- conditioning on when inflation is realized timing dummy
- exclusion of whole COVID period

## Results: Bias in Survey Data, 4 Quarters Ahead

 $\epsilon_{t,h} = \mu_{h} + \theta_{h} G\left(S_{t};\gamma\right) + u_{t+h|t}$ 

Source	ECB	SPF	Consensus
	Pane	l A: Linear I	Model
$\mu$	0.16	0.11	0.14
	(0.13)	(0.14)	(0.13)
$R^2$	0.00	0.00	0.00
RMSFE	0.82	0.80	0.80
	Panel B: S	state Depend	lent Model
$\mu$	-0.09	-0.12	0.06
	(0.17)	(0.17)	(0.15)
$\theta$	$0.46^{*}$	0.42	0.14
	(0.26)	(0.26)	(0.26)
$\gamma$	1.80	1.80	1.80
$R^2$	0.05	0.05	0.00
$\mu + \theta$	0.37	0.30	0.20
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Table: Note: Bias in Survey Data, 4 Quarters Ahead.  $R^2$  is the adjusted  $R^2$ . Newey-West standard errors are in parenthesis. Stars denote the 10% (\*), 5% (\*\*) and 1% (\*\*\*) significance level. RMSFE of naive 1.8% forecast is 0.79. The SPF survey is usually conducted in the second half of the first month of each quarter. Consensus forecasts are elicited on the

second month of the quarter.

(6)

## Conclusions

- We document three novel findings regarding the ECB inflation forecasts:
  - a systematic bias towards the target, which implies over (under) prediction when inflation is low (high);
  - ▶ a larger bias when inflation is above the target
  - bias larger at medium horizons
- Results robust to:
  - assumption on information set
  - excluding COVID sample
- How can we explain the state dependent bias?
  - external assumptions not enough

#### Further Investigation

- dynamics of forecasting models
- expert judgement/strategic communication motives

ECB Projections Under Scrutiny

## **ECB Forecasting Is A Joke**

Jan. 21, 2019 6:48 AM ET | FXE, VGK, EUO

# Bruegel: ECB's huge forecasting errors undermine credibility of current forecasts

In the past five years ECB forecasts have proven to be systematically incorrect. Such forecast errors raise serious doubts about the reliability of the ECB's current forecast. By Konstantinos Efstathiou and Francesco Papadia 12 December 2018

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Testing for bias (methodological):

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       ECB vs FED

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- ▶ ECB (till July 2021): keep inflation below, but close to 2%.
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## Inflation Above Threshold



Figure: Actual year-over -year Harmonized Index of Consumer Prices Inflation (HICP), solid blue line, estimated threshold, red solid line, quarters in which observed inflation  $S_t$  is above the threshold, grey shaded areas.

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## SPF Long Term Inflation Expectations

#### Longer-term inflation expectations



## Outline

#### Testing Framework

State Dependent Bias and Efficiency

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- Alternative Tests
- ▶ Implementation Details
- ► Bias:
  - ResultsExternal Assumptions
  - Robustness
- ► Efficiency:
  - Results
  - Discussion

#### Conclusions

## Testing for State Dependent Forecast Performance

▶ Test of state dependent forecast performance by Odendahl et al. (2022)

$$Loss_{t,h} = X'_t \mu_h + X'_t \theta_h G\left(S_t; \gamma_h\right) + u_{t+h|t} \tag{7}$$

with  $X_t$  a  $(k_1 \times 1)$  vector of explanatory variables,  $S_t$  observable variable introducing state dependence,  $\gamma_h$  a parameter,  $G(\cdot)$  a nonlinear function.

Null hypothesis of unbiasedness:

$$E\left(Loss_{t,h}\right) = 0\tag{8}$$

Alternative

$$E\left(Loss_{t,h}\right) = X'_{t}\mu_{h} + X'_{t}\theta_{h}G\left(S_{t};\gamma_{h}\right)$$

$$\tag{9}$$

$$H_0: \mu_h = \theta_h = 0 \qquad H_A: \mu_h \neq 0, \theta_h \neq 0 \tag{10}$$

Advantages

 Other tests lack power against the alternative of parametric state dependence (Giacomini and Rossi, 2010; Amisano and Giacomini, 2007)

#### ▶ Inference:

- Problem of a nuisance parameter (threshold) that is present only under the alternative, which makes standard asymptotic inference invalid
- ► Critical values cannot be tabulated, need to simulate them

## Testing for State Dependent Bias: Previous Studies

Same null hypothesis of unbiasedness:

$$E\left(\epsilon_{t,h}\right) = 0\tag{11}$$

Alternative

$$E\left(\epsilon_{t,h}\right) = \mu_h + \theta_h G\left(S_{t+h};\gamma^*\right) \tag{12}$$

- Differences with our approach
  - $\blacktriangleright~S_{t+h},$  variable that defines the state observed when target variable is realized
  - $\blacktriangleright$   $S_{t+h}$  usually *output*
  - $G(S_{t+h}; \gamma^*)$  is a dummy variable that takes value one if  $S_{t+h} \ge \gamma^*$  with  $\gamma^*$  chosen by the researcher

Questions:

- previous studies: did the FED under/over predict inflation in its projections made in 2008Q1 for 2009Q1, given that we observe a negative output gap in 2009Q1?
- our study: will the ECB under/over predict inflation for 2009Q1 in its projections made in 2008Q1, given that in 2008Q1 the ECB observes that inflation is high?



## Results: Bias

$$\epsilon_{t,h} = y_{t+h} - y_{t+h|t} = \mu_h + \theta_h G(S_t; \gamma_h) + u_{t+h|t}$$
(13)

				Forecas	st Horizon			
			Single				Poe	oled
h =	0	1	2	3	4	5	0 - 5	0 - 8
			Р	anel A: I	inear M	odel		
$\mu_h$	-0.02	0.04	0.09	0.14	0.16	0.18	$0.10^{**}$	$0.09^{*}$
	(0.01)	(0.04)	(0.07)	(0.10)	(0.13)	(0.14)	(0.05)	(0.05)
$R^2$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
			Panel	B: State	Depende	nt Mode	el	
$\mu_h$	0.01	-0.03	-0.07	-0.07	-0.09	-0.07	-0.05	-0.03
	(0.04)	(0.05)	(0.10)	(0.14)	(0.17)	(0.18)	(0.05)	(0.06)
$\theta_h$	-0.08*	0.14*	$0.29^{**}$	$0.39^{**}$	$0.46^{*}$	0.45	$0.28^{***}$	$0.22^{***}$
	(0.04)	(0.08)	(0.14)	(0.19)	(0.26)	(0.29)	(0.08)	(0.08)
$\gamma_h$	2.27	1.80	1.80	1.80	1.80	1.80	1.80	1.80
p-val	0.14	0.16	0.06	0.06	0.16	0.14	0.05	0.06
$R^2$	0.07	0.02	0.06	0.07	0.06	0.05	0.05	0.02

## Bias Sample 1999Q4-2019Q4

				Forecas	t Horizon						
			Single				Poe	oled			
h =	0	1	2	3	4	5	0 - 5	0 - 8			
	Panel A: Linear Model										
	0.00	0.05	с 10 Г	anel A: I	inear wi	ouer	0 10**	0.10*			
$\mu_h$	-0.02	0.05	0.10	0.14	0.16	0.17	$0.10^{**}$	$0.10^{*}$			
	(0.01)	(0.04)	(0.07)	(0.11)	(0.14)	(0.14)	(0.05)	(0.05)			
$R^2$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00			
			Panel I	B: State	Depende	nt Mode	el				
$\mu_h$	0.01	0.00	-0.02	-0.06	-0.07	-0.08	-0.04	-0.03			
	(0.04)	(0.05)	(0.09)	(0.13)	(0.16)	(0.18)	(0.05)	(0.05)			
$\theta_h$	-0.08**	0.10	$0.23^{*}$	0.38*	0.42	0.46	$0.25^{***}$	$0.19^{***}$			
	(0.04)	(0.08)	(0.14)	(0.20)	(0.27)	(0.29)	(0.08)	(0.08)			
$\gamma_h$	2.27	1.81	1.81	1.81	1.81	1.80	1.81	1.81			
p - val	0.14	0.27	0.10	0.08	0.22	0.14	0.00	0.02			
$R^2$	0.07	0.00	0.03	0.05	0.05	0.02	0.04	0.01			

Table: Note:  $R^2$  is the adjusted  $R^2$ . Newey-West standard errors are in parenthesis. Stars denote the 10% (\*), 5% (\*\*) and 1% (\*\*\*) significance level.

#### ▶ back

## Bias: Known Threshold

$$\epsilon_{t,h} = y_{t+h} - y_{t+h|t} = \mu_h + \theta_h d\left(S_t > \gamma^*\right) + u_{t+h|t} \tag{14}$$

$ \begin{array}{c c c c c c c c c c c c c c c c c c c $									
$h = \frac{Single}{0 \ 1 \ 2 \ 3 \ 4 \ 5 \ 0-5 \ 0-8} \frac{Pooled}{0 \ 1 \ 2 \ 3 \ 4 \ 5 \ 0-5 \ 0-8}$					Forecas	st Horizon			
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$				Single				Poo	oled
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	h =	0	1	2	3	4	5	0 - 5	0 - 8
$\begin{array}{c c c c c c c c c c c c c c c c c c c $									
$\begin{array}{cccccccccccccccccccccccccccccccccccc$			Р	anel A: S	tate Dep	endent N	Aodel: $\gamma$	= 1.8	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$\mu$	0.00	-0.03	-0.07	-0.07	-0.09	-0.07	-0.05	-0.03
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		(0.02)	(0.05)	(0.10)	(0.14)	(0.18)	(0.20)	(0.06)	(0.07)
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$\theta$	-0.03	0.14*	0.29**	0.39**	0.46*	0.45*	0.28***	0.22***
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		(0.03)	(0.07)	(0.13)	(0.19)	(0.25)	(0.27)	(0.08)	(0.09)
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$R^2$	0.00	0.02	0.06	0.07	0.06	0.05	0.05	0.02
$\begin{array}{c c c c c c c c c c c c c c c c c c c $									
$\begin{array}{cccccccccccccccccccccccccccccccccccc$			Р	anel B: S	tate Dep	endent N	Iodel: $\gamma$	= 1.9	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$\mu$	0.00	0.02	0.04	0.07	0.14	0.15	0.07	0.07
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		(0.02)	(0.05)	(0.09)	(0.14)	(0.18)	(0.20)	(0.06)	(0.06)
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$\theta$	-0.04	0.05	0.11	0.17	0.06	0.07	0.07	0.05
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		(0.03)	(0.07)	(0.14)	(0.21)	(0.27)	(0.29)	(0.09)	(0.10)
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$R^2$	0.01	0.00	0.00	0.00	0.00	0.00	0.00	0.00
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $									
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$			Р	anel C: S	tate Dep	endent N	Iodel: $\gamma$	= 1.7	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$\mu$	0.00	-0.03	-0.06	-0.08	-0.09	-0.09	-0.06	-0.04
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		(0.02)	(0.05)	(0.10)	(0.15)	(0.19)	(0.20)	(0.06)	(0.07)
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$\theta$	-0.03	0.13*	0.28**	0.39**	0.45*	0.48*	0.28***	0.24 * * *
$R^2$ 0.00 0.02 0.06 0.07 0.05 0.06 0.05 0.03		(0.03)	(0.07)	(0.13)	(0.20)	(0.25)	(0.27)	(0.08)	(0.09)
	$R^2$	0.00	0.02	0.06	0.07	0.05	0.06	0.05	0.03

Table: Note:  $R^2$  is the adjusted  $R^2$ . Newey-West standard errors are in parenthesis. Stars denote the 10% (\*), 5% (\*\*) and 1% (\*\*\*) significance level.

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## Results: Bias When Inflation Realized

$$\epsilon_{t,h} = y_{t+h} - y_{t+h|t} = \mu_h + \theta_h G(S_{t+h};\gamma) + u_{t+h|t}$$
(15)

				Foreca	st Horizon						
			Single				Poo	oled			
h =	0	1	2	3	4	5	0 - 5	0 - 8			
	Panel A: Linear Model										
$\mu$	-0.02	0.04	0.09	0.14	0.16	0.18	0.10**	$0.09^{*}$			
	(0.01)	(0.04)	(0.07)	(0.10)	(0.13)	(0.14)	(0.05)	(0.05)			
$R^2$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00			
	Panel B: State Dependent Model										
$\mu$	0.01	-0.06	-0.20	-0.32	-0.44*	-0.51*	-0.28***	-0.44***			
θ	(0.04) - $0.08^*$	(0.08) $0.24^{***}$	(0.14) $0.60^{***}$	(0.21) $0.96^{***}$	(0.28) $1.28^{***}$	(0.31) $1.41^{***}$	(0.08) $0.74^{***}$	(0.08) $0.99^{***}$			
	(0.04)	(0.08)	(0.12)	(0.17)	(0.20)	(0.20)	(0.08)	(0.08)			
$\gamma$	2.27	1.87	1.84	1.89	1.94	1.94	1.84	1.81			
p - val	0.14	0.03	0.00	0.00	0.00	0.00	0.00	0.00			
$R^2$	0.07	0.07	0.21	0.36	0.45	0.52	0.27	0.37			

Table: Note:  $R^2$  is the adjusted  $R^2$ . Newey-West standard errors are in parenthesis. Stars denote the 10% (\*), 5% (\*\*) and 1% (\*\*\*) significance level.

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## Bias: Alternative Observed Inflation: I

			Sir	ıgle			Poo	oled
h =	0	1	2	3	4	5	0 - 5	0 - 8
				Panel A	: Nowca	st		
$\mu$	0.00	-0.02	-0.07	-0.09	-0.09	-0.11	-0.06***	$-0.04^{***}$
	(0.04)	(0.06)	(0.10)	(0.14)	(0.17)	(0.18)	(0.05)	(0.06)
$\theta$	-0.06	0.11	$0.29^{***}$	$0.42^{***}$	$0.46^{*}$	$0.52^{**}$	$0.29^{***}$	$0.24^{***}$
	(0.04)	(0.08)	(0.13)	(0.18)	(0.24)	(0.26)	(0.07)	(0.08)
$\gamma$	2.30	1.80	1.80	1.80	1.80	1.80	1.80	1.80
$p_{val}$	0.25	0.23	0.05	0.03	0.14	0.10	0.00	0.01
$R^2$	0.03	0.01	0.07	0.08	0.06	0.08	0.06	0.03
			Pa	nel B: Ex	-Post Re	alized		
$\mu$	0.00	-0.03	-0.06	-0.07	-0.07	-0.05	-0.05	-0.00
	(0.03)	(0.06)	(0.10)	(0.14)	(0.17)	(0.17)	(0.05)	(0.05)
$\theta$	-0.04	$0.14^{*}$	0.30***	0.43***	$0.46^{*}$	0.44*	0.28***	0.20***
	(0.03)	(0.08)	(0.13)	(0.18)	(0.24)	(0.25)	(0.07)	(0.08)
$\gamma$	1.88	1.87	1.87	1.87	1.87	1.87	1.87	1.92
$p_{val}$	0.33	0.18	0.05	0.03	0.15	0.14	0.00	0.00
$R^2$	0.01	0.03	0.07	0.09	0.06	0.05	0.06	0.02

## Bias: Alternative Observed Inflation: II

			Sing	gle			Poo	oled
h =	0	1	2	3	4	5	0 - 5	0 - 8
		_						
		Pa	anel C: Fi	rst Month	of Curr	ent Quar	ter	
$\mu$	0.00	-0.02	-0.05	-0.07	-0.05	-0.05	-0.04	-0.00
	(0.03)	(0.05)	(0.09)	(0.13)	(0.16)	(0.17)	(0.05)	(0.05)
$\theta$	-0.05*	$0.12^{*}$	$0.27^{***}$	$0.40^{***}$	0.39	0.42	$0.26^{***}$	$0.19^{***}$
	(0.02)	(0.07)	(0.13)	(0.18)	(0.25)	(0.27)	(0.07)	(0.08)
$\gamma$	2.22	1.76	1.76	1.76	1.76	1.71	1.76	1.79
$p_{val}$	0.28	0.22	0.07	0.04	0.20	0.15	0.00	0.01
$R^2$	0.01	0.12	0.23	0.38	0.48	0.56	0.28	0.38
			Panel	D: Last	Chree M	onths		
$\mu$	0.01	-0.03	-0.08	-0.09	-0.07	-0.01	-0.05	-0.03
	(0.04)	(0.05)	(0.10)	(0.14)	(0.18)	(0.19)	(0.05)	(0.06)
$\theta$	-0.08***	0.14*	0.31***	0.43***	0.46*	0.45	0.28***	0.22***
	(0.04)	(0.07)	(0.13)	(0.19)	(0.25)	(0.28)	(0.08)	(0.08)
$\gamma$	2.23	1.67	1.67	1.67	1.78	1.78	1.78	1.78
$p_{val}$	0.11	0.15	0.04	0.04	0.15	0.14	0.00	0.01
$R^2$	0.01	0.01	0.05	0.07	0.04	0.04	0.04	0.02

			Sing	e			Poo	oled
h =	0	1	2	3	4	5	0 - 5	0 - 8
			Panel A:	March l	Forecasts	s, Linear		
$\mu$	-0.03	$0.19^{***}$	$0.20^{**}$	0.11	0.11	0.26	$0.14^{***}$	$0.12^{**}$
	(0.02)	(0.07)	(0.10)	(0.14)	(0.18)	(0.21)	(0.06)	(0.06)
$R^2$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
		р	anal B. F	)	Forest	ta Linor		
	0.05	0.00	0 15	0.12	0.06		0.05	0.06
$\mu$	(0.03)	-0.09	(0.13)	(0.12)	(0.20)	(0.20)	(0.05)	(0.06)
$R^2$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
		Pane	l C: Mare	ch Foreca	asts, Sta	te Deper	ndent	
$\mu$	-0.02	0.10	0.03	-0.08	-0.05	0.09	0.01	0.01
	(0.02)	(0.09)	(0.12)	(0.17)	(0.23)	(0.26)	(0.07)	(0.07)
$\theta$	-0.03	0.18	$0.35^{**}$	0.39	0.32	0.34	$0.29^{***}$	$0.24^{***}$
	(0.05)	(0.13)	(0.17)	(0.25)	(0.33)	(0.38)	(0.10)	(0.11)
$R^2$	0.02	0.07	0.16	0.12	0.04	0.04	0.07	0.03
		Denel I	D. Decem	han Fand	anata Si	ata Dan	andont	
	0.01	Fallel 1	D: Decen		casts, 5	ate Dep	endent	0.01
$\mu$	-0.01	-0.09	-0.08	-0.08	-0.22	-0.12	-0.09	-0.01
0	(0.03)	(0.14)	(0.16)	(0.21)	(0.29)	(0.2)	(0.08)	(0.08)
θ	-0.13***	0.00	0.40**	0.32	0.45	0.33	0.23***	0.14
<b>D</b> <sup>2</sup>	(0.05)	(0.18)	(0.20)	(0.26)	(0.36)	(0.37)	(0.10)	(0.11)
$R^2$	0.24	0.00	0.16	0.05	0.08	0.04	0.04	0.01

## Bias: March vs December Forecasts

### **Results:** Bias and External Assumptions

ı =	0	1	2	3	4	5	0 - 5	0 - 8
			Pa	anel A: Int	erest Rate	es		
$\iota_{1,h}$	0.00	-0.04	-0.08	-0.09	-0.12	-0.11	-0.07	-0.04
-,	(0.02)	(0.05)	(0.10)	(0.15)	(0.19)	(0.21)	(0.06)	(0.07)
h	-0.03	0.16***	0.33***	0.45 * * *	0.55 * * *	0.55 * *	0.32***	0.30***
	(0.03)	(0.07)	(0.14)	(0.20)	(0.25)	(0.27)	(0.09)	(0.09)
2.h	-0.11	0.22	0.27*	0.26	0.23	0.15	0.17**	0.19***
	(0.21)	(0.15)	(0.17)	(0.17)	(0.18)	(0.17)	(0.08)	(0.06)
$\mathcal{C}^2$	0.00	0.04	0.11	0.11	0.10	0.08	0.08	0.08
			Pa	nel B: Exc	hange Ra	te		
$\iota_{1,h}$	0.00	-0.05	-0.08	-0.10	-0.13	-0.10	-0.07	-0.03
-,	(0.02)	(0.06)	(0.10)	(0.15)	(0.19)	(0.20)	(0.06)	(0.07)
h	-0.03	0.16***	0.30***	0.42**	0.48*	0.41	0.28***	0.15*
	(0.03)	(0.08)	(0.14)	(0.20)	(0.26)	(0.29)	(0.09)	(0.09)
2.h	-0.39	-0.93	0.12	-0.02	-0.50	1.17	0.66	$1.72^{***}$
_,	(1.01)	(0.71)	(0.83)	(1.02)	(1.14)	(1.17)	(0.49)	(0.42)
$R^2$	0.00	0.03	0.06	0.06	0.07	0.09	0.07	0.09
				Panel C: 0	Oil Prices			
$\iota_{1.h}$	0.00	-0.03	-0.10	-0.14	-0.19	-0.21	-0.11*	-0.11
	(0.02)	(0.04)	(0.09)	(0.14)	(0.19)	(0.20)	(0.06)	(0.07)
h	-0.02	0.08	0.26**	0.40**	0.50**	0.56**	0.29***	0.26***
	(0.03)	(0.06)	(0.13)	(0.19)	(0.25)	(0.27)	(0.08)	(0.09)
$l_{2,h}$	0.01***	0.01***	0.01***	0.01*	0.01	0.01	0.01***	0.01***
, -	(0.00)	(0.00)	(0.00)	(0.01)	(0.01)	(0.01)	(0.00)	(0.00)
${}^2$	0.07	0.41	0.21	0.14	0.12	0.13	0.15	0.09

 $\epsilon_{t,h} = \mu_{1,h} + \mu_{2,h}\zeta_{t,h} + \theta_h G\left(S_t;\gamma\right) + u_{t+h|t}$ (16)

Table: Note:  $R^2$  is the adjusted  $R^2$ . Newey-West standard errors are in parenthesis. Stars denote the 10% (\*), 5% (\*\*) and 1% (\*\*\*) significance level. The state dependent model assumes that the threshold  $\gamma_b$  is known and fixed at 1.80. (back)  $d^2 > d^2 >$ 

## **Results:** Bias and External Assumptions

 $\epsilon_{t,h} = \mu_{1,h} + \mu_{2,h}\zeta_{t,h} + \theta_{1,h}G\left(S_t;\gamma^*\right) + \theta_{2,h}G\left(S_t;\gamma^*\right)\zeta_{t,h} + u_{t+h|t}$ 

h =	0	1	2	3	4	5	0 - 5	0 - 8
			1	Panel A. In	torest Bate			
41 h	0.00	-0.04	-0.08	-0.08	-0.10	-0.09	-0.06	-0.04
1.1.1	(0.02)	(0.05)	(0.10)	(0.14)	(0.19)	(0.21)	(0.06)	(0.07)
$\theta_{1,h}$	-0.03	0.16***	0.32***	0.43***	0.52***	0.50*	0.30***	0.30***
1,/1	(0.03)	(0.07)	(0.13)	(0.19)	(0.25)	(0.28)	(0.09)	(0.10)
$\mu_{2h}$	0.24	0.12	0.38*	0.47	0.46	0.34	0.41***	0.17
	(0.60)	(0.29)	(0.28)	(0.30)	(0.34)	(0.38)	(0.16)	(0.15)
$\theta_{2h}$	-0.40	0.15	-0.16	-0.32	-0.30	-0.23	-0.32*	0.02
	(0.64)	(0.34)	(0.34)	(0.36)	(0.40)	(0.42)	(0.18)	(0.17)
$R^2$	0.00	0.03	0.10	0.12	0.10	0.08	0.10	0.08
			F	Panel B: Ex	change Ra	te		
$\mu_{1,h}$	0.00	-0.04	-0.09	-0.09	-0.11	-0.08	-0.07	-0.02
. 1,/1	(0.02)	(0.06)	(0.10)	(0.15)	(0.19)	(0.21)	(0.06)	(0.07)
$\theta_{1,h}$	-0.03	0.16***	0.30***	0.43**	0.48*	0.42	0.28***	0.15*
	(0.03)	(0.08)	(0.14)	(0.21)	(0.26)	(0.28)	(0.09)	(0.09)
$\mu_{2,h}$	-0.40	-0.75	-0.59	0.24	1.76	3.07	0.70	2.03***
	(1.84)	(1.02)	(1.14)	(1.39)	(1.67)	(1.78)	(0.71)	(0.65)
$\theta_{2,h}$	0.03	-0.35	1.51	-0.55	-1.07	-1.03	-0.08	-0.52
	(2.20)	(1.42)	(1.66)	(2.05)	(2.27)	(2.35)	(0.97)	(0.84)
$R^2$	0.00	0.02	0.06	0.05	0.06	0.08	0.07	0.09
				Panel C:	Oil Prices			
$\mu_{1h}$	0.00	-0.03	-0.10	-0.14	-0.19	-0.21	-0.11*	-0.11
	(0.02)	(0.04)	(0.10)	(0.14)	(0.19)	(0.20)	(0.06)	(0.07)
$\theta_{1h}$	-0.02	0.07	0.25**	0.41**	0.50**	0.56**	0.29***	0.26***
	(0.03)	(0.06)	(0.13)	(0.19)	(0.25)	(0.28)	(0.08)	(0.09)
$\mu_{2,h}$	0.01	0.01***	0.01	0.01*	0.01	0.01	0.01***	0.01***
	(0.00)	(0.00)	(0.01)	(0.01)	(0.01)	(0.01)	(0.00)	(0.00)
$\theta_{2,h}$	0.00	0.00	0.01	-0.01	0.00	0.00	0.00	0.00
	(0.01)	(0.00)	(0.01)	(0.01)	(0.01)	(0.02)	(0.01)	(0.01)
$R^2$	0.06	0.41	0.20	0.13	0.11	0.11	0.15	0.09

Table: Note:  $R^2$  is the adjusted  $R^2$ . Newey-West standard errors are in parenthesis. Stars denote the 10% (\*), 5% (\*\*) and 1% (\*\*\*) significance level. The state dependent model

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(17)

## Bias in Exogenous Assumptions: Short Term Rate

$$\zeta_{t,h} = y_{t+h} - y_{t+h|t} = \mu_h + \theta_h G(S_t; \gamma_h) + u_{t+h|t}$$
(18)

				Forecas	t Horizon			
			Single				Poo	oled
h =	0	1	2	3	4	5	0 - 5	0 - 8
			-					
			1	Panel A: I	linear M	odel		
$\mu_h$	-0.01	-0.03	-0.05	-0.10	-0.19	-0.26	-0.11***	-0.24***
	(0.01)	(0.03)	(0.06)	(0.09)	(0.12)	(0.14)	(0.04)	(0.06)
$R^2$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
		1	Panel B: S	State Depe	endent M	odel, Fiz	$\mathbf{ked} \gamma$	
$\mu_h$	0.00	0.00	-0.01	-0.03	-0.08	-0.15	-0.04	-0.15*
	(0.01)	(0.05)	(0.10)	(0.14)	(0.18)	(0.21)	(0.06)	(0.09)
$\theta_h$	-0.03	-0.06	-0.07	-0.13	-0.19	-0.19	-0.11	-0.16
	(0.02)	(0.07)	(0.13)	(0.18)	(0.23)	(0.28)	(0.08)	(0.12)
$R^2$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
		Pa	nel C: Sta	ate Depen	dent Mo	del, Unk	nown $\gamma$	
$\mu_h$	0.01	0.02	0.02	0.03	0.00	-0.07	0.00	-0.11
	(0.02)	(0.07)	(0.13)	(0.19)	(0.27)	(0.34)	(0.09)	(0.12)
$\theta_h$	-0.03*	-0.12*	-0.20**	-0.36**	-0.53*	-0.55	-0.29***	-0.38***
	(0.01)	(0.08)	(0.14)	(0.18)	(0.24)	(0.29)	(0.08)	(0.10)
$\gamma_h$	1.81	2.01	2.10	2.13	2.13	2.13	2.13	2.13
p - val	0.47	0.43	0.53	0.30	0.16	0.19	0.01	0.00
$R^2$	0.03	0.03	0.03	0.07	0.11	0.08	0.07	0.05

## Bias in Exogenous Assumptions: Exchange Rate

$$\zeta_{t,h} = y_{t+h} - y_{t+h|t} = \mu_h + \theta_h G(S_t; \gamma_h) + u_{t+h|t}$$
(19)

				Forec	ast Horizo	n		
			Single				Po	oled
h =	0	1	2	3	4	5	0 - 5	0 - 8
				Panel A:	Linear N	Iodel		
$\mu_h$	0.00	0.00	0.01	0.01	0.01	0.02	0.01	0.01
	(0.00)	(0.01)	(0.01)	(0.02)	(0.02)	(0.02)	(0.01)	(0.01)
$R^2$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
			Panel B:	State De	pendent I	Model, Fix	ed $\gamma$	
$\mu_h$	0.00	-0.01	-0.01	-0.03	-0.02	-0.03	-0.02***	-0.03***
	(0.00)	(0.01)	(0.02)	(0.02)	(0.03)	(0.03)	(0.01)	(0.01)
$\theta_h$	0.00	$0.02^{*}$	0.03	0.07***	0.07**	0.09***	0.05***	0.07***
	(0.00)	(0.01)	(0.02)	(0.03)	(0.03)	(0.03)	(0.01)	(0.01)
$R^2$	0.00	0.02	0.02	0.08	0.07	0.11	0.07	0.10
		P	anel C: S	state Depe	ndent M	odel, Unkr	nown $\gamma$	
$\mu_{h}$	0.00	-0.01	-0.01	-0.02	-0.02	-0.03	-0.01	-0.02*
	(0.00)	(0.01)	(0.02)	(0.02)	(0.03)	(0.03)	(0.01)	(0.01)
$\theta_h$	0.01*	$0.02^{*}$	0.04	0.06**	0.07*	0.09**	0.04***	0.07***
	(0.00)	(0.01)	(0.02)	(0.03)	(0.04)	(0.04)	(0.01)	(0.01)
$\gamma_h$	1.83	1.80	1.81	1.81	1.81	1.81	1.83	1.83
p - val	0.30	0.34	0.39	0.20	0.21	0.13	0.00	0.00
$R^2$	0.02	0.02	0.02	0.06	0.07	0.12	0.05	0.09

## Bias in Exogenous Assumptions: Oil Prices

$$\zeta_{t,h} = y_{t+h} - y_{t+h|t} = \mu_h + \theta_h G(S_t; \gamma_h) + u_{t+h|t}$$
(20)

	Forecast Horizon									
	Single							Pooled		
h =	0	1	2	3	4	5	0 - 5	0 - 8		
			F	Panel A:	Linear M	odel				
$\mu_h$	0.50	1.62	1.13	0.99	1.01	0.87	1.01	1.10*		
	(0.47)	(1.75)	(2.00)	(1.98)	(2.15)	(2.22)	(0.76)	(0.65)		
$R^2$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00		
		P	anel B: S	tate Dep	endent N	Iodel, Fiz	$\mathbf{ced} \gamma$			
$\mu_h$	0.43	-1.20	-2.10	-2.36	-0.84	-0.12	-1.00	-0.24		
	(0.70)	(2.39)	(2.77)	(2.82)	(3.19)	(3.33)	(1.08)	(0.94)		
$\theta_h$	0.12	5.22	5.91	5.89	3.35	1.79	3.65 * * *	2.40*		
	(0.94)	(3.26)	(3.75)	(3.73)	(4.28)	(4.47)	(1.45)	(1.26)		
$R^2$	0.00	0.01	0.00	0.00	0.00	0.00	0.01	0.00		
		Pan	el C: Sta	te Deper	dent Mo	del, Unk	nown $\gamma$			
$\mu_h$	1.10	-1.88	-2.10	-1.90	2.46	-1.38	-1.00	-0.33		
	(0.00)	(0.01)	(0.02)	(0.02)	(0.03)	(0.03)	(0.01)	(0.01)		
$\theta_h$	-1.98	6.34*	5.91	5.34**	-5.35*	4.39**	3.65 * * *	$2.85^{***}$		
	(0.00)	(0.01)	(0.02)	(0.03)	(0.04)	(0.04)	(0.01)	(0.01)		
$\gamma_h$	2.18	1.71	1.81	1.83	2.20	1.84	1.81	1.84		
p - val	0.17	0.08	0.39	0.53	0.67	0.42	0.02	0.03		
$R^2$	0.02	0.02	0.00	0.00	0.00	0.00	0.01	0.01		

## Results: Bias for Random Walk Model

$$\epsilon_{t,h} = y_{t+h} - y_{t+h|t} = \mu_h + \theta_h G\left(S_t; \gamma_h\right) + u_{t+h|t} \tag{21}$$

				Foreca	ast Horizon			
		Poo	Pooled					
h =	0	1	2	3	4	5	0 - 5	0 - 8
				Panel A:	Linear Mo	del		
11.5	0.03	0.04	0.04	0.04	0.04	0.06	0.04	0.03
μn	(0.07)	(0.09)	(0.12)	(0.15)	(0.17)	(0.19)	(0.06)	(0.06)
$R^2$	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
			Panel B	: State Der	oendent Mo	odel. Fixed	$\gamma$	
$\mu_h$	0.03	0.06	0.11	0.26	0.33	0.41	0.20***	$0.34^{***}$
	(0.10)	(0.13)	(0.18)	(0.22)	(0.25)	(0.27)	(0.09)	(0.09)
$\theta_{h}$	0.01	-0.05	-0.13	-0.41	-0.53	-0.64*	-0.28***	-0.57***
12	(0.14)	(0.18)	(0.24)	(0.30)	(0.34)	(0.36)	(0.12)	(0.12)
$R^2$	0.00	0.00	0.00	0.02	0.04	0.06	0.02	0.08
			Panel C: S	State Depe	ndent Mod	el, Unknow	n γ	
$\mu_h$	0.06	0.10	0.15 * * *	0.27***	0.36***	0.43***	0.20***	0.30***
	(0.04)	(0.05)	(0.10)	(0.14)	(0.17)	(0.18)	(0.05)	(0.06)
$\theta_h$	-0.11	-0.24*	-0.44***	-0.88***	-1.05***	-1.06***	-0.60***	-0.81***
	(0.04)	(0.08)	(0.14)	(0.19)	(0.26)	(0.29)	(0.08)	(0.08)
$\gamma_h$	2.29	2.27	2.27	2.27	2.18	2.13	2.27	2.13
p - val	0.78	0.41	0.11	0.04	0.01	0.01	0.00	0.00
$R^2$	0.00	0.00	0.04	0.13	0.20	0.20	0.09	0.14

## ECB Projections during COVID



Figure: Actual year-over -year Harmonized Index of Consumer Prices Inflation (HICP), solid blue line with marker, and ECB Quarterly Projections for 2020Q1-2022Q3, grey lines. Projections are produced for the current and following two calendar years, i.e. up to eleven quarters ahead in Q1 and for at most eight quarters ahead in Q4.