

# Should the ECB Adjust its Strategy in the Face of a Lower $r^*$ ?<sup>1</sup>

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<sup>1</sup>The views expressed here do not necessarily represent those of the Banque de France, the Eurosystem, the Federal Reserve Bank of Boston or the Federal Reserve System.

# Motivation

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- Implications for monetary policy  $\Rightarrow$  higher ELB incidence, given an unchanged strategy
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  - Should the inflation target be raised, given an unchanged policy rule?
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- This paper: *quantitative* analysis based on an estimated NK model of the euro area economy
- Follow up on the U.S.-based analysis in Andrade et al. (2020)

## Preview of Main Findings

- Given the estimated rule, the current inflation target ( $\pi^* \lesssim 2\%$ ) is suboptimal if  $r^* < 2\%$
- Keeping that rule unchanged, a 1% decrease in  $r^*$  calls for a 0.9% increase in  $\pi^*$  ( $1.7\% \Rightarrow 2.6\%$ )
- Alternatives to raising the inflation target:
  - aggressive countercyclical fiscal policy
  - modifying the rule to incorporate a sufficiently strong "make-up" component

## Related literature

- Quantitative analyses of  $\pi^*$ : Khan et al. (2003), Schmitt-Grohé and Uribe (2010), Amano et al. (2009), Carlsson and Westermarck (2016), Bilbiie et al. (2014), Ascari et al. (2015), Adam and Weber (2019), Lepetit (2018),...
- Quantitative analyses of  $\pi^*$  with a ZLB/ELB constraint: Coibion et al. (2012), Dordal-i-Carreras et al. (2016), Kiley and Roberts (2017), Blanco (2016),...
- Our contribution: explicit analysis of the relation between  $r^*$  and  $\pi^*$
- Main caveat: "within the model" analysis

# The Model

- Medium-scale NK model
- Non-zero trend inflation
- Staggered price and wage setting à la Calvo
- Imperfect indexation of prices to lagged price inflation; and of wages to lagged price inflation and productivity.
- Shocks: risk premium, marginal utility of consumption, technology, monetary policy, price and wage markups
- Trend growth  $\Rightarrow r^* = \rho + \mu_z$
- Baseline monetary policy rule

$$i_t = \max\{i_t^n, e\}$$

$$i_t^n = (1 - \rho_i)i + \rho_i i_{t-1}^n + (1 - \rho_i) [a_\pi(\pi_t - \pi) + a_x x_t] + \zeta_{r,t}$$

with  $i = r^* + \pi$  and where  $\pi$  defines the *inflation target* ( $\neq \mathbb{E}\{\pi_t\}$ )

# Solution Method

- 1 Detrending of non-stationary quantities by technology parameter
- 2 Log-linearization around deterministic steady state.
- 3 Solution under the ZLB as in Bodenstein et al. (2009) and Guerrieri and Iacoviello (2015)

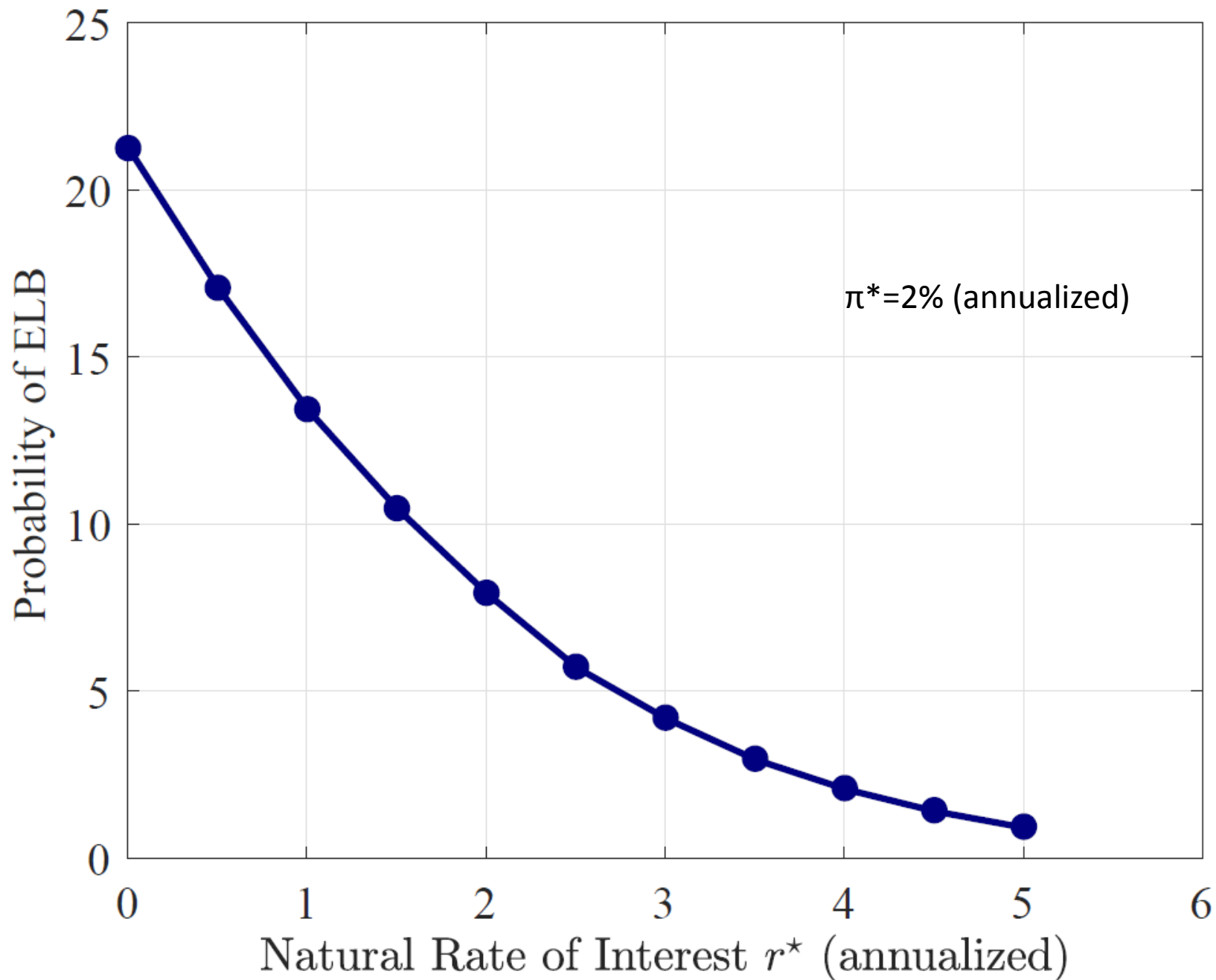


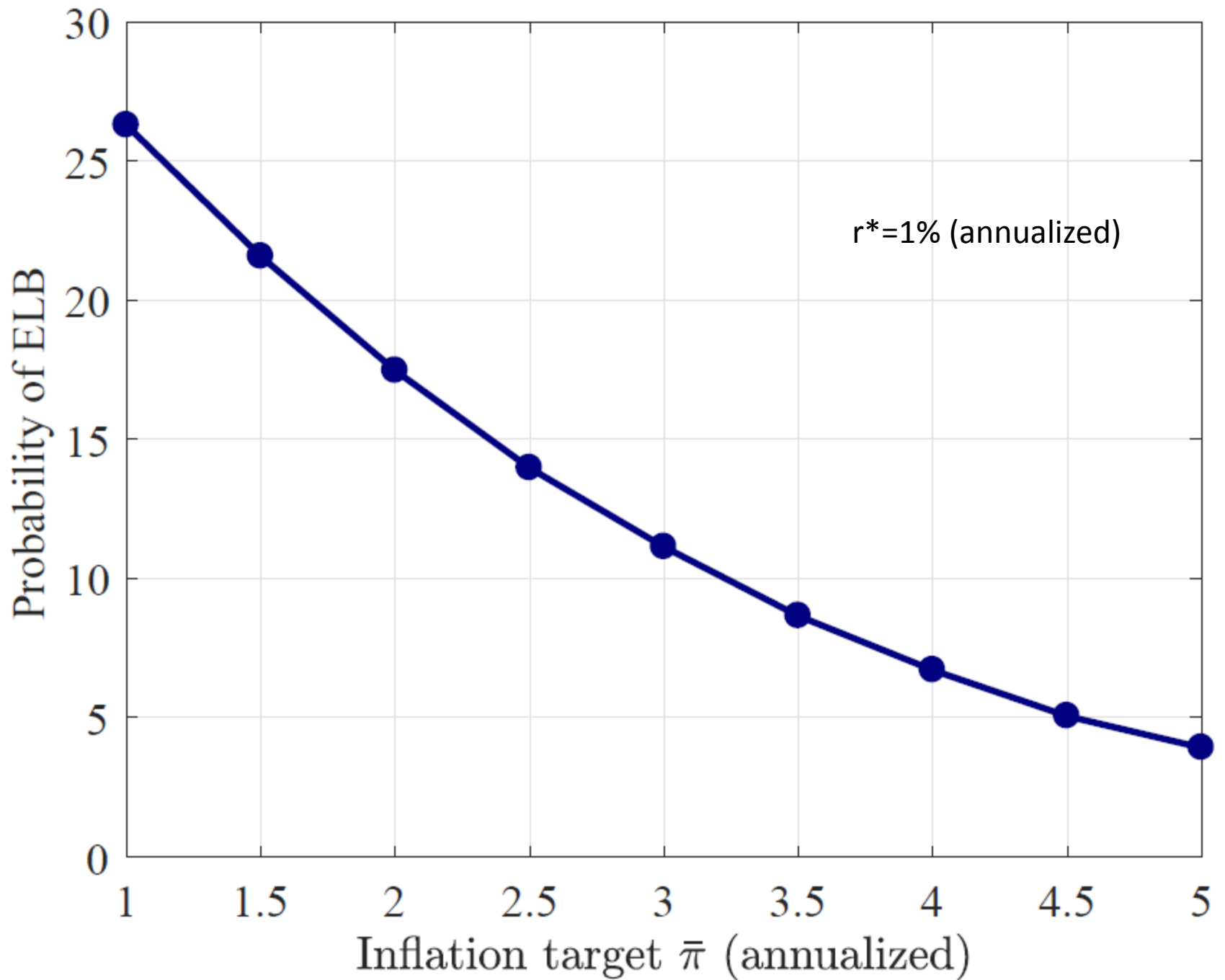
# Calibration and Estimation

- Calibrated parameters:  $1/\phi = 0.7$  ;  $\theta_p = 6$  ;  $\theta_w = 3$  ;  $e = -0.5/4$
- Remaining parameters estimated using Bayesian approach on the model without ZLB and sample period 1985Q1-2014Q4
- Gaussian priors for  $(\rho, \mu_z, \pi)$  with means consistent with inflation, GDP growth and real rate averages.
- Vector of observables:

$$x_t = [\Delta \log GDP_t, \Delta \log GDP \text{ Deflator}_t, \Delta \log Wage_t, \text{Short term rate}_t]$$

- Some model properties





# The Optimal Inflation Target

- Second order approximation to household expected utility:  $\mathcal{W}(\pi; \theta)$
- The *optimal inflation target*

$$\pi^*(\theta) = \arg \max_{\pi} \mathcal{W}(\pi; \theta)$$

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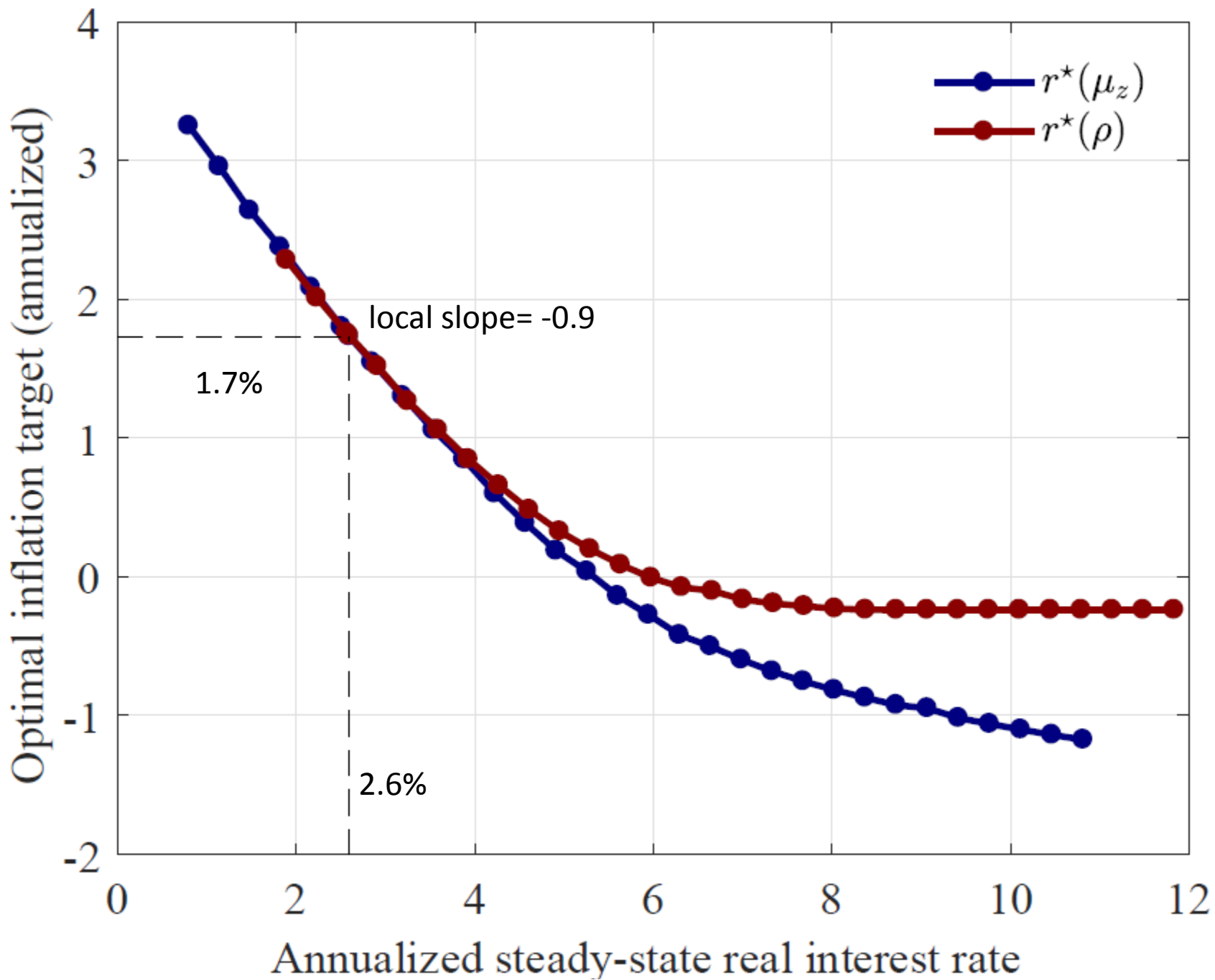
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- The baseline  $(r^*, \pi^*)$  relation:

(a) varying  $\mu_z$

(b) varying  $\rho$

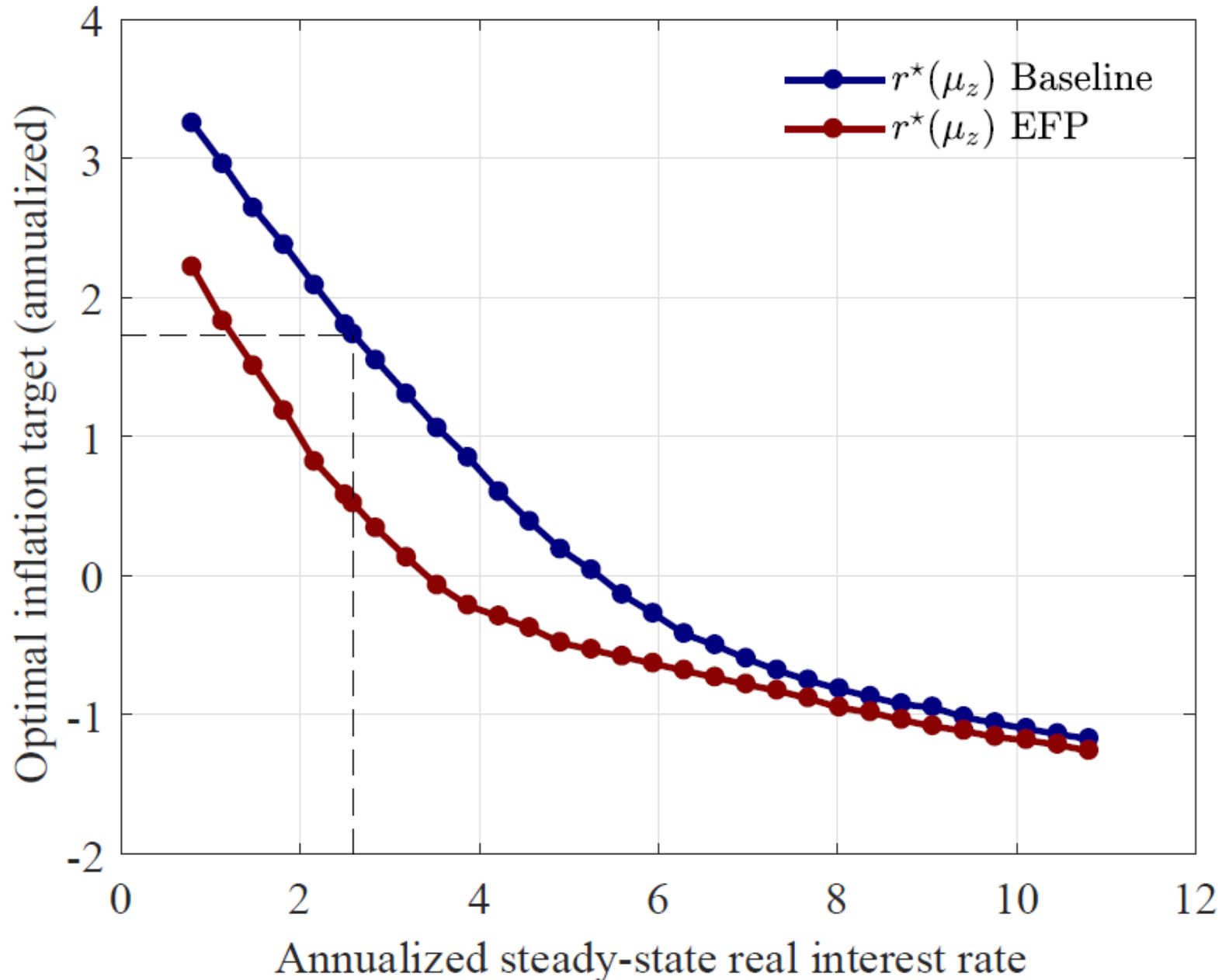
while keeping other parameters at their posterior mean



## Alternative Strategies

- Emergency Fiscal Package (4% of output,  $\rho_g = 0.85$ , triggered when cumulative output gap is  $-6\%$ )

# Emergency Fiscal Package

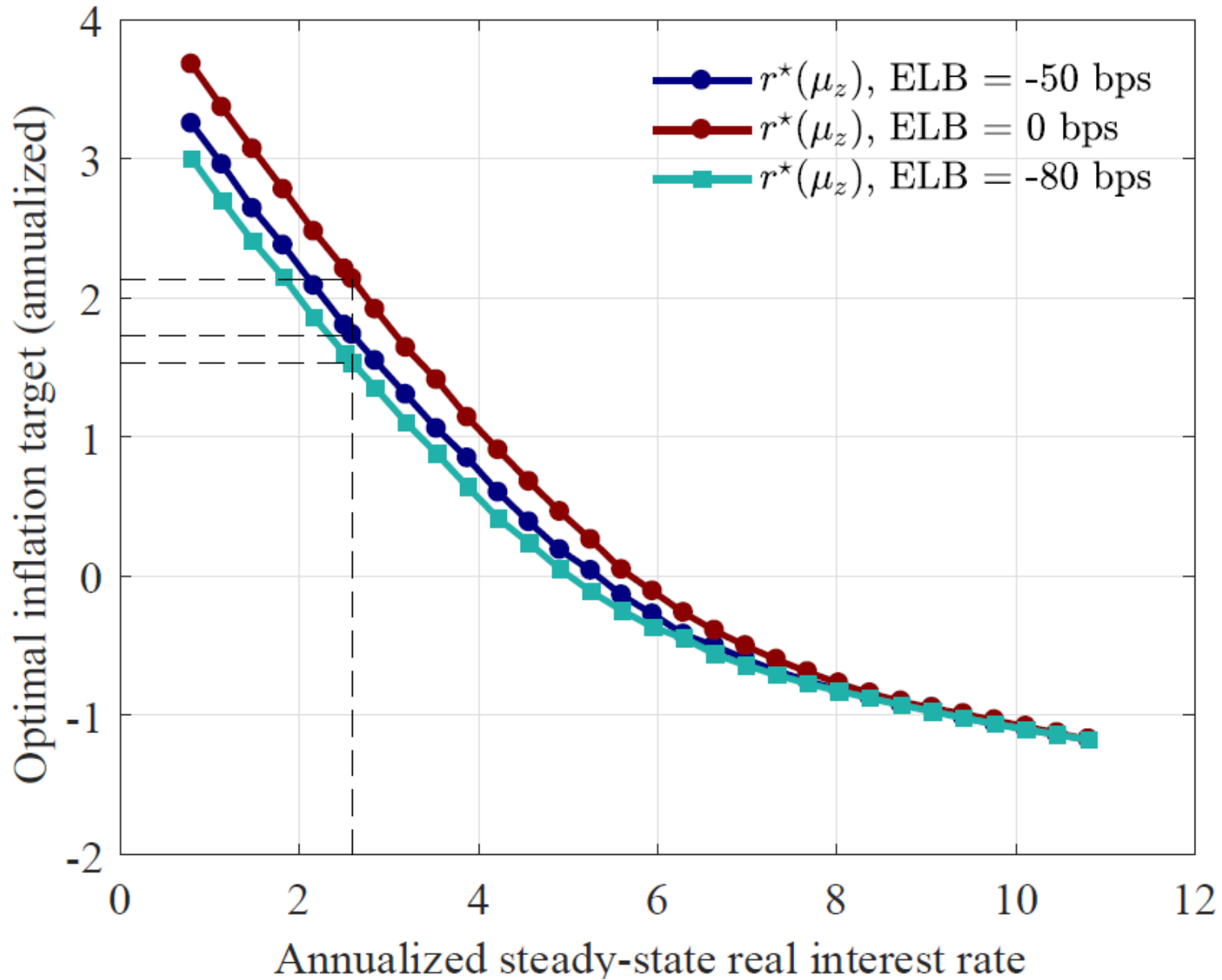




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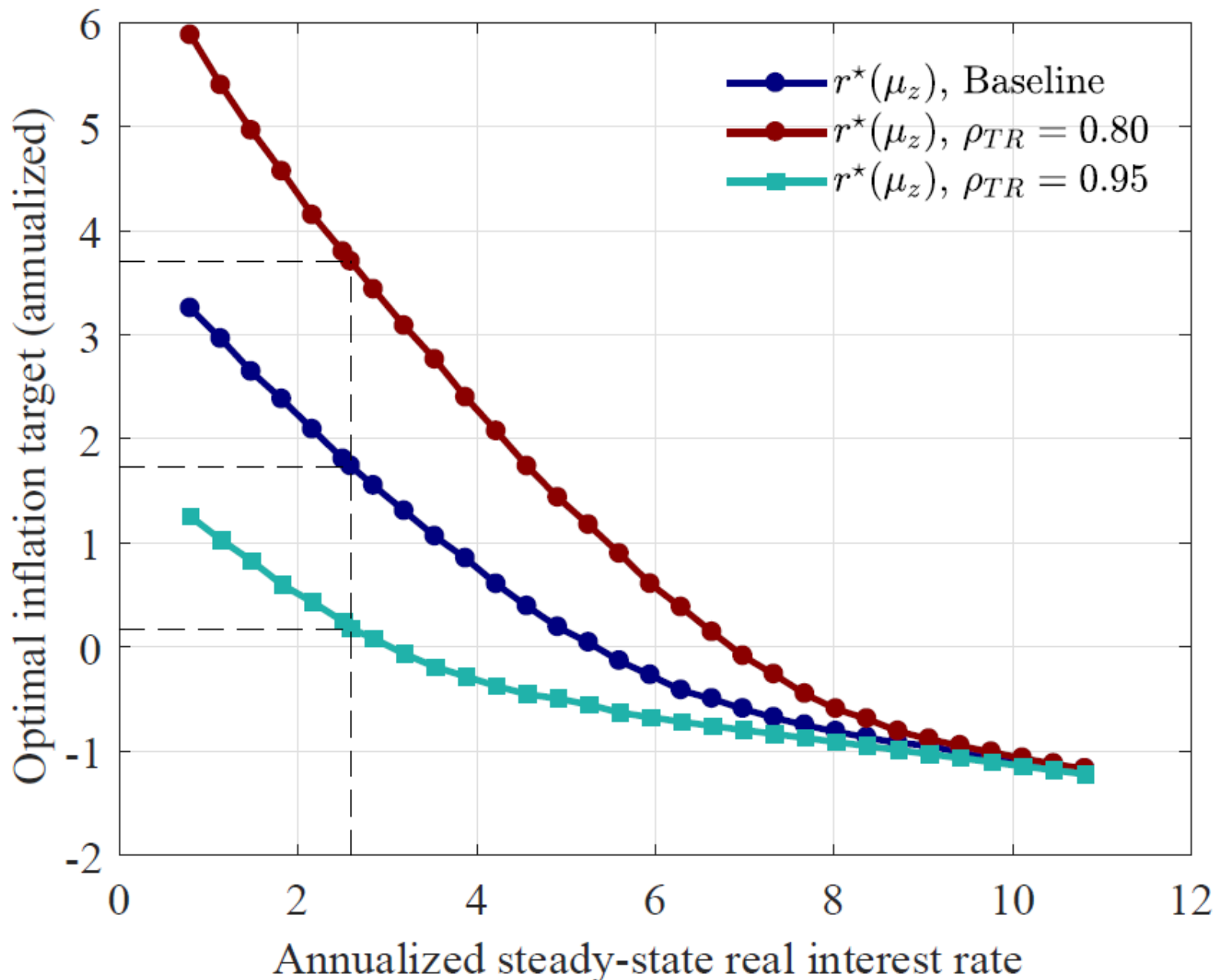
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# Alternative Inertia Coefficients



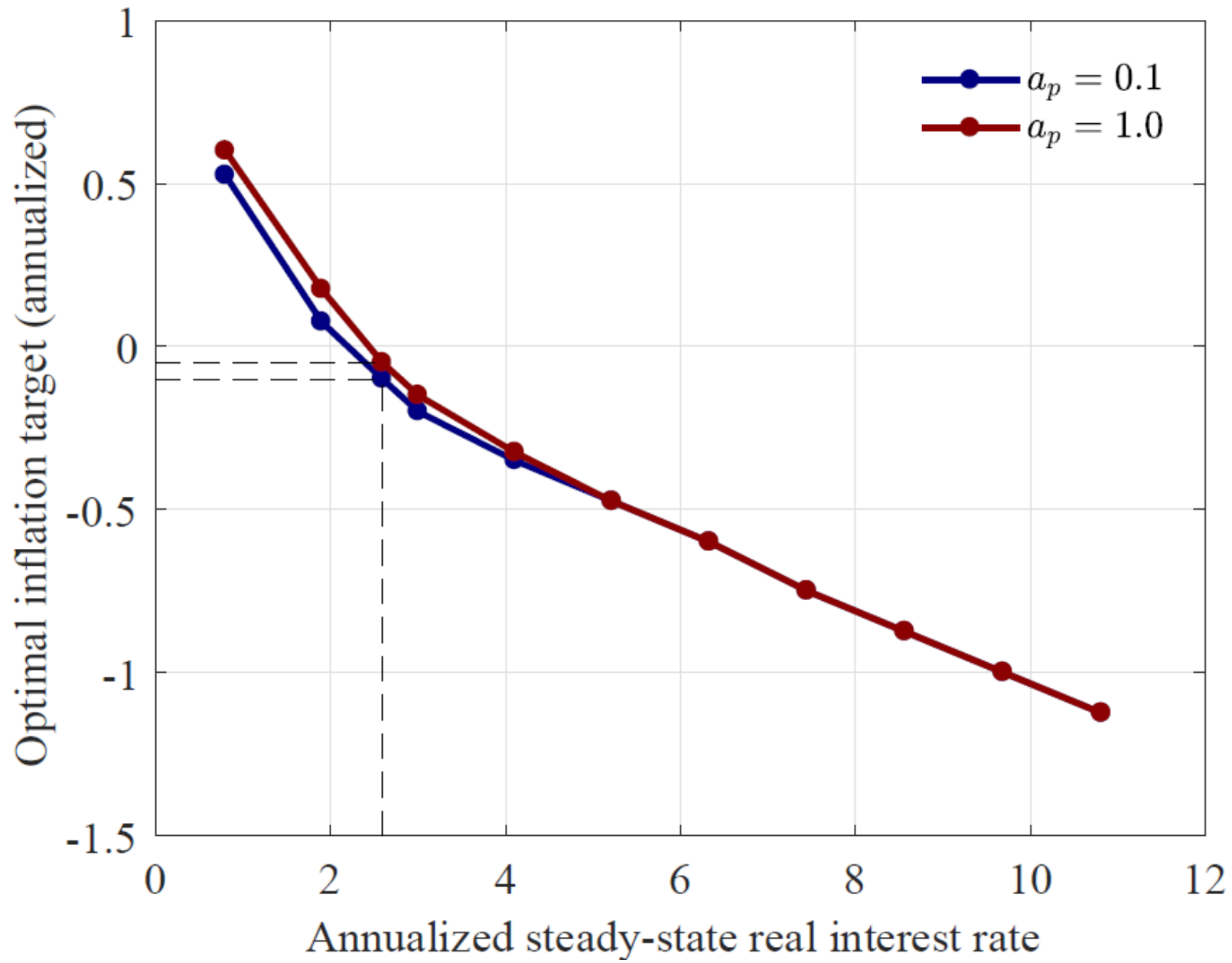
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- Price level targeting:

$$i_t^n - i = \rho_i (i_{t-1}^n - i) + (1 - \rho_i) [a_p (p_t - p_t^*) + a_x x_t] + \zeta_{r,t}$$

where  $p_t^* = p_0 + \pi \cdot t$  and  $a_p \in \{0.1, 0.5\}$

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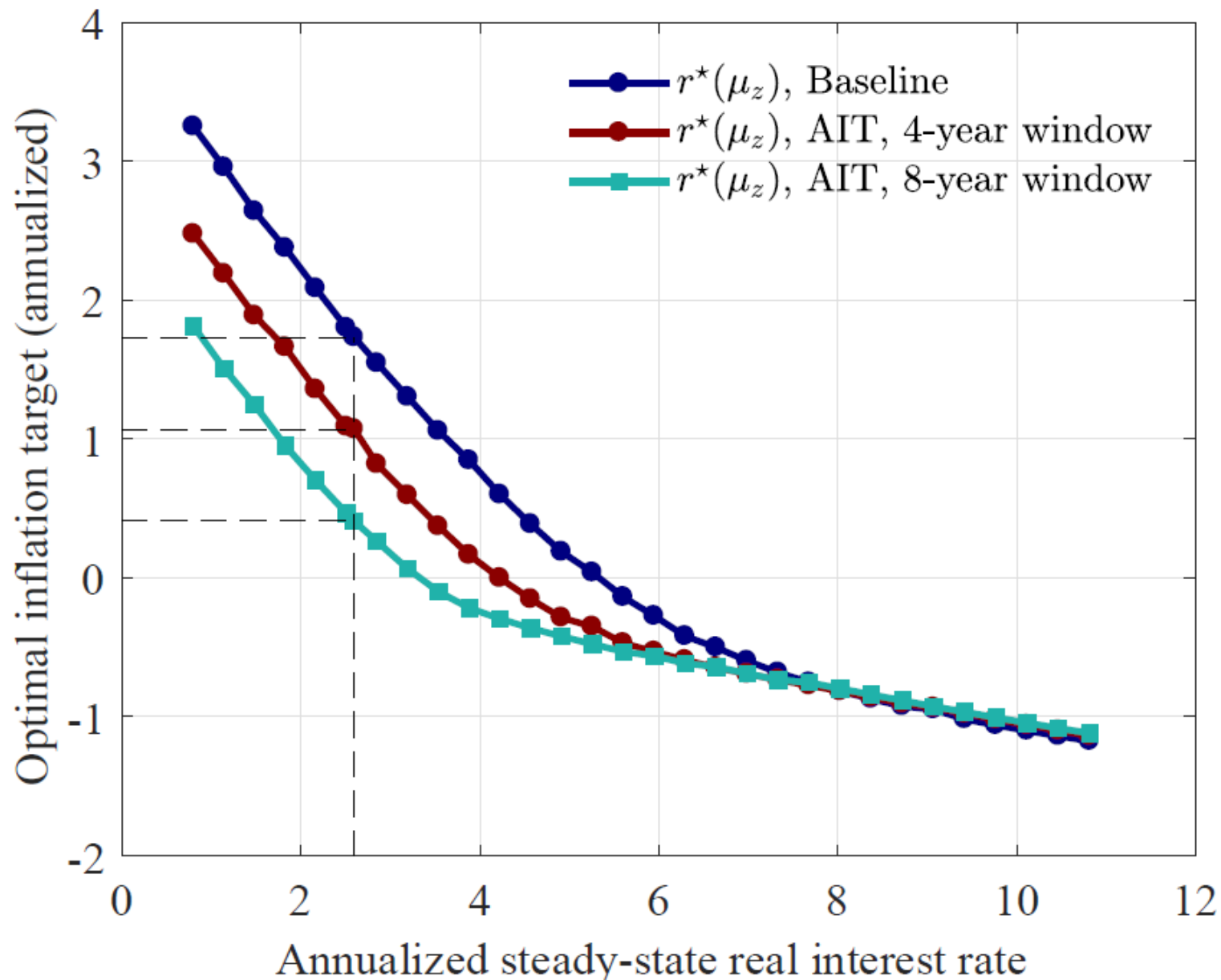
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- Average inflation targeting:

$$i_t^n - i = \rho_i (i_{t-1}^n - i) + (1 - \rho_i) [a_p (\pi_t^a - \pi) + a_x x_t] + \zeta_{r,t}$$

where  $\pi_t^a = (1/H) \sum_{h=0}^{H-1} \pi_{t-h}$  and  $H \in \{1, 16, 32\}$

# Average Inflation Targeting





# Summary and Conclusions

- Quantitative assessment of the optimal inflation target in the euro area, as a function of  $r^*$  and under an ELB constraint.
- Under the baseline estimated policy rule, a (local) decline in  $r^*$  calls for a *close to one-for-one* (0.9) increase in the inflation target  $\Rightarrow$  marginal costs of inflation are low compared to the stabilization benefits of a higher nominal rate
- If  $r^*$  has declined significantly and the rule is unchanged, the current "below but close to 2%" target is suboptimal
- Alternatives to a higher inflation target:
  - more aggressive countercyclical fiscal policies
  - more aggressive "lower for longer" forward guidance
  - average inflation targeting

# The Model

- Representative household with preferences:

$$\mathbb{E}_t \sum_{s=0}^{\infty} \beta^s \left\{ e^{\zeta_{g,t+s}} \log(C_{t+s} - \eta C_{t+s-1}) - \frac{\chi}{1+\nu} \int_0^1 N_{t+s}(h)^{1+\nu} dh \right\}$$

and budget constraint

$$P_t C_t + e^{\zeta_{q,t}} Q_t B_t \leq \int_0^1 W_t(h) N_t(h) dh + B_{t-1} - T_t + D_t$$

- Final goods: perfect competition with technology

$$Y_t = \left( \int_0^1 Y_t(f)^{(\theta_p-1)/\theta_p} df \right)^{\theta_p/(\theta_p-1)}$$

- Intermediate goods: monopolistic competition with technology

$$Y_t(f) = Z_t L_t(f)^{1/\phi}$$

where  $Z_t = Z_{t-1} e^{\mu_z + \zeta_{z,t}}$

# The Model

- Price setting à la Calvo, with stochastic subsidies  $\zeta_{u,t}$ , and partial indexation

$$P_t(f) = \Pi_{t-1}^{\gamma_p} P_{t-1}(f)$$

- Wage setting à la Calvo, with partial indexation

$$W_t(h) = e^{\gamma_z \mu_z} \Pi_{t-1}^{\gamma_w} W_{t-1}(h)$$

- Interest rate rule:

$$i_t = \max\{i_t^n, 0\}$$

where

$$i_t^n - i = \rho_i (i_{t-1}^n - i) + (1 - \rho_i) [a_\pi (\pi_t - \pi) + a_y (y_t - y_t^n)] + \zeta_{r,t}$$

with  $i = \rho + \mu_z + \pi$  and where  $\pi$  defines the *inflation target*.

## An Incorrect Argument

- "The effects of a decline in  $r^*$ , independently of its source, can be exactly offset by a commensurate increase in the inflation target  $\pi$ "

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- "The effects of a decline in  $r^*$ , independently of its source, can be exactly offset by a commensurate increase in the inflation target  $\pi$ "
- The argument ignores:
  - (i) An increase in inflation has (permanent) welfare costs of its own.
  - (ii) Changes in  $\rho$  and  $\mu_z$  have different effects on wage inflation (given  $\pi$ )
  - (iii) Changes in  $(\rho, \mu_z)$  affect the equilibrium dynamics independently of  $\pi$

These are the effects that we seek to evaluate.

Table 1: Estimation Results

Parameter	Prior Shape	Prior Mean	Priod std	Post. Mean	Post. std	Low	High
$\rho$	Normal	0.20	0.05	0.20	0.05	0.12	0.27
$\mu_z$	Normal	0.50	0.05	0.45	0.04	0.38	0.52
$\pi$	Normal	0.80	0.05	0.79	0.05	0.71	0.86
$\alpha_p$	Beta	0.66	0.05	0.63	0.04	0.56	0.69
$\alpha_w$	Beta	0.66	0.05	0.60	0.04	0.54	0.66
$\gamma_p$	Beta	0.50	0.15	0.10	0.04	0.03	0.16
$\gamma_w$	Beta	0.50	0.15	0.29	0.10	0.12	0.45
$\gamma_z$	Beta	0.50	0.15	0.50	0.15	0.26	0.75
$\eta$	Beta	0.70	0.15	0.72	0.03	0.67	0.78
$\nu$	Gamma	1.00	0.20	0.95	0.18	0.64	1.24
$a_\pi$	Gamma	2.00	0.15	2.10	0.13	1.87	2.31
$a_y$	Gamma	0.50	0.05	0.50	0.05	0.41	0.58
$\rho_i$	Beta	0.85	0.10	0.86	0.02	0.84	0.89
$\sigma_z$	Inverse Gamma	0.25	1.00	0.87	0.14	0.63	1.10
$\sigma_m$	Inverse Gamma	0.25	1.00	0.11	0.01	0.10	0.12
$\sigma_q$	Inverse Gamma	0.25	1.00	0.22	0.06	0.14	0.30
$\sigma_c$	Inverse Gamma	0.25	1.00	0.24	0.04	0.18	0.31
$\sigma_u$	Inverse Gamma	0.25	1.00	0.20	0.11	0.06	0.35
$\rho_m$	Beta	0.25	0.10	0.37	0.06	0.26	0.47
$\rho_z$	Beta	0.25	0.10	0.24	0.10	0.09	0.39
$\rho_c$	Beta	0.85	0.10	0.99	0.00	0.99	1.00
$\rho_q$	Beta	0.85	0.10	0.95	0.02	0.91	0.98
$\rho_u$	Beta	0.80	0.10	0.80	0.10	0.66	0.96

Note: 'std' stands for Standard Deviation, 'Post.' stands for Posterior, and 'Low' and 'High' denote the bounds of the 90% probability interval for the posterior distribution. Values for parameters  $\rho$ ,  $\mu_z$ ,  $\pi$  are expressed in percent, in quarterly (not annualized) terms.

Table 2: Properties of the Model

Policy Parameters			Moments				
$e$	$r^*$	$\bar{\pi}$	$E(\pi^a)$	$std(\pi^a)$	$E(x)$	$std(x)$	P(ELB)
-0.50	1.00	2.00	1.49	4.58	-0.30	2.00	17.47
-0.50	1.00	3.00	2.83	2.91	-0.12	1.14	11.13
-0.50	2.00	2.00	1.84	2.80	-0.11	1.15	10.73
-0.50	2.00	3.00	2.94	2.31	-0.04	0.82	6.25
-0.50	3.00	2.00	1.95	2.25	-0.04	0.84	5.88
-0.50	3.00	3.00	2.98	2.13	-0.01	0.71	3.30

**Note:** Results from simulations of the model under various values of  $r^*$  and  $\bar{\pi}$ , an ELB at  $e = -.5$ , and the remaining model parameters at their estimated posterior mean.  $\pi^a$  denotes the year-on-year inflation rate,  $x$  is the output gap,  $E(\cdot)$  stands for mean,  $std(\cdot)$  stands for Standard Deviation, P(ELB) denotes the unconditional probability of hitting the ELB.

