

# **Passive Funds Actively Affect Prices: Evidence from the Largest ETF Markets**

Karamfil Todorov

London School of Economics and Political Science

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- Recent years have seen a surge in passive investment
  - ETFs: \$0.2 trillion of AUM in 2004; \$5 trillion in 2018
  - Commoditization makes investing simple and cost-efficient, but could reduce price informativeness and create systemic risks
- ETFs in VIX and commodities – beneficial setting to study price impact of passive funds
  - Larger fraction of the market compared to stocks. VIX: 25%, S&P 500: <2%
  - Easier to measure non-fundamental price distortions
  - Price impact of different types of trading. Leverage-induced trading

# Preview of main results

- **ETFs affect prices** of underlying assets
  - Trading demand from ETFs is strongly related to prices
  - Propose a model-independent approach to replicate the value of a VIX futures. Isolate **non-fundamental part of the VIX futures premium** of 18.5 % p.a., strongly related to ETF demands
- **Decompose ETF demands**
  - Calendar rebalancing
  - Flow rebalancing
  - Leverage rebalancing
- **Analyze the risk of leverage rebalancing**
  - Amplifies price changes and introduces unhedgeable risks for ETF counterparties
  - Document **new ETF anomaly**: trading against leverage rebalancing earns large abnormal returns and SR-s above two across markets
  - Puzzling: exposed to 'right-way risk'

# Isolate ETF-induced price distortions

- ETF price impact manifests itself through an increase in the non-fundamental part of prices
- **Model-independent** approach for replicating the fundamental value of a VIX futures contract
  - Construct a synthetic futures contract from option prices
  - **No** parametric or distributional **assumptions**: simply use the definition of variance. Robust to jumps
- Price of the replicated contract was close to that of the traded one before the introduction of ETFs but diverged consistently thereafter
- The **gap** between the two prices (18.5% per year, on average) is **strongly related to ETF demand**

# ETF demand decomposition

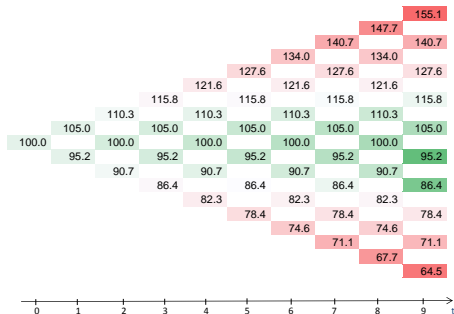
- Propose a novel **decomposition** of **ETF demand**
- **Calendar rebalancing**: arises because futures are finite-maturity instruments. ETFs have to gradually roll their exposure
- **Flow rebalancing**: driven by fund flows
- **Leverage rebalancing**: arises due to the maintenance of a constant daily leverage by leveraged ETFs
  - Leveraged ETFs aim to deliver multiples of the daily return of their benchmark index. E.g., if the benchmark index goes up by 10%, a two-times leveraged ETF should return 20%.
  - New type of mechanic institutional demand
  - Has the **largest effects** on the gap

# Leverage rebalancing

- **Amplifies price changes:** ETFs mechanically have to buy after price increases and sell after price decreases
- Trading against leveraged ETFs
  - Providing liquidity to investors with short horizons, who follow momentum-like strategy
  - **Introduces unhedgeable risks** for ETF counterparties (negative convexity)
- Potential distorting effect on prices can be large even in a market with a 0 net share of ETFs
  - VIX in February 2018: net market share of ETFs was close to 0
  - But potential price impact due to leverage rebalancing was **60% of the total market** size

# Understanding the risks of leverage rebalancing

- Take an arbitrageur who trades against a pair of equal-sized **ETFs with opposite leverages** (e.g.,  $L = 2$  and  $L = -2$ )
  - Is she perfectly hedged by matching  $L = 2$  demand with  $L = -2$ ?  
No!
  - **Not a zero-return** strategy, but a **bet on variance**
  - Lose from price jumps, gain from small price fluctuations (contrarian)



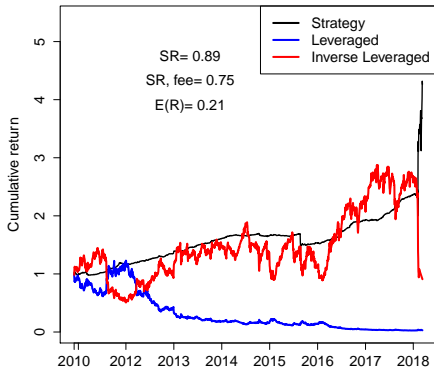
# Understanding the risks of leverage rebalancing

- **Hedging** the variance exposure is not easy
- Propose a simple strategy to understand the risks of trading against leverage rebalancing
- Document a **novel ETF-related anomaly** across markets
  - Short a pair of ETFs with opposite leverages (e.g., 2 and -2), to approximate liquidity provision to leveraged ETFs
  - Surprisingly, the returns on such a strategy are not zero, but are consistently positive across markets.  $\alpha$  of 16.6% for VIX, 42.3 % for natural gas. SR of 0.89 and 2.59
  - Puzzling: exposed to 'right-way risk'

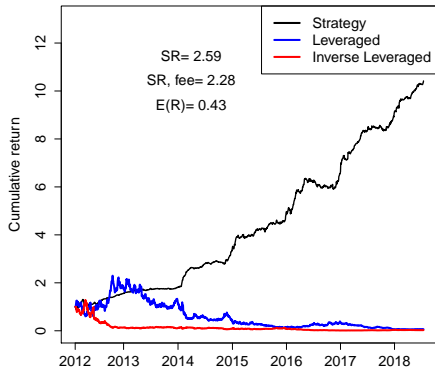


# The short-both strategy – intra-day returns

VIX



Gas



# Implications

- **Price is strongly related to ETF demand**, when ETFs control a large share of the market
  - Leverage-induced rebalancing creates a feedback effect on prices
  - Contributes to the policy debate on the desirability of commoditization and the general shift towards passive investing
- **More nuanced view of VIX** and the VIX futures premium
  - VIX and its derivatives – barometer of financial stress, used in various risk models
  - But prices are significantly disrupted by non-fundamental mechanical ETF demand
- **Novel decomposition** of ETF trading demand. Develop a strategy to capture the risk premium of leverage rebalancing

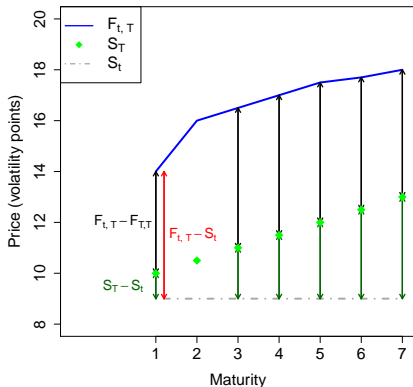
Thank you for your attention and useful comments!

# Appendix

- VIX and commodity ETFs obtain price exposure by entering into futures contracts
  - follow a benchmark based on the first two futures contracts
  - roll daily
- Some ETFs also aim to maintain a constant *daily* leverage ratio,  $L$ 
  - Example: benchmark return is 10%, a double-leveraged ( $L = 2$ ) ETF should return 20%; an inverse ETF ( $L = -1$ ) should return -10%

# VIX futures prices – informative about fundamentals?

- Test whether  $F_{t,T}$  is informative about the fundamental spot at maturity  $S_T$ , or is influenced by premiums
- Use the identity  $F_{t,T} - S_t = F_{t,T} - F_{T,T} + S_T - S_t$
- Check whether today's (negative) basis  $F_{t,T} - S_t$  predicts changes of the futures ( $F$ ) or the spot VIX ( $S$ ), or both



# Predictive power of basis

- Basis of short maturities **predicts futures** but **not spot**
- Front end of the futures curve is mostly influenced by ETFs

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Spot VIX on basis:  $S_T - S_t = \alpha_1 + \beta_1 \cdot (F_{t,T} - S_t) + \epsilon_{1,t}$

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	T=1m	T=2m	T=3m	T=4m	T=5m	T=6m	T=7m	T=8m
$\beta_1$	0.02	0.27	0.64***	0.72***	0.84***	0.94***	0.98***	1.01***
R <sup>2</sup>	0.00	0.03	0.09	0.10	0.14	0.18	0.23	0.27

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VIX futures on basis:  $F_{T,T} - F_{t,T} = \alpha_2 + \beta_2 \cdot (F_{t,T} - S_t) + \epsilon_{2,t}$

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	T=1m	T=2m	T=3m	T=4m	T=5m	T=6m	T=7m	T=8m
$\beta_2$	-0.98***	-0.73***	-0.36***	-0.28***	-0.16***	-0.06**	-0.02	0.01
R <sup>2</sup>	0.14	0.10	0.04	0.04	0.02	0.01	0.00	0.00

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Synthetic

Basis regressions

# VIX ETF Futures gap (EFG)

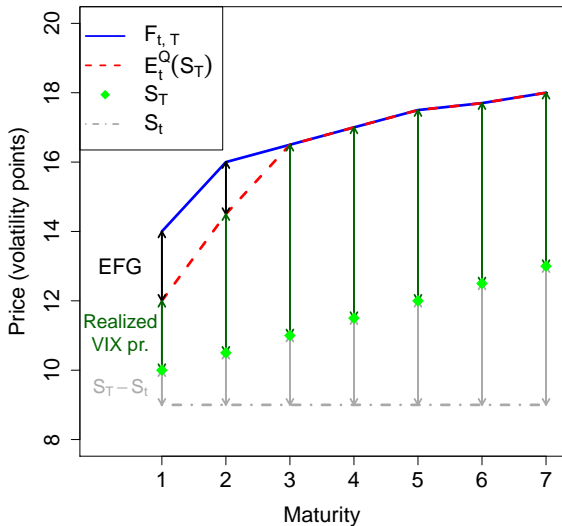
- Decompose basis into premiums and spot change:

$$F_{t,T} - S_t = \underbrace{F_{t,T} - E_t^Q(S_T)}_{\text{ETF Futures gap (EFG)}} + \underbrace{E_t^Q(S_T) - S_T}_{\text{Realized VIX Premium}} + \underbrace{S_T - S_t}_{\text{Spot VIX change}}$$

- $F_{t,T}$  is influenced by ETF demand
- $E_t^Q(S_T)$  – fundamental value, computed from a non-ETF-influenced market
- $F_{t,T} - E_t^Q(S_T) \neq 0$  due to **market segmentation**.  
Non-fundamental **ETF futures gap (EFG)**



# VIX ETF Futures gap (EFG)



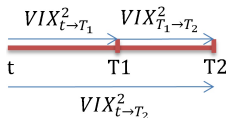
# Computing $E_t^Q(S_T) = E_t^Q(VIX_{T_1 \rightarrow T_2})$

- Using the definition of variance:

$$\begin{aligned}\text{Var}_t^Q(VIX_{T_1 \rightarrow T_2}) &= E_t^Q(VIX_{T_1 \rightarrow T_2}^2) - \left(E_t^Q(VIX_{T_1 \rightarrow T_2})\right)^2 \\ \iff E_t^Q(VIX_{T_1 \rightarrow T_2}) &= \sqrt{E_t^Q(VIX_{T_1 \rightarrow T_2}^2) - \text{Var}_t^Q(VIX_{T_1 \rightarrow T_2})}\end{aligned}$$

- First term under the square root is forward  $VIX_{T_1 \rightarrow T_2}^2$ :

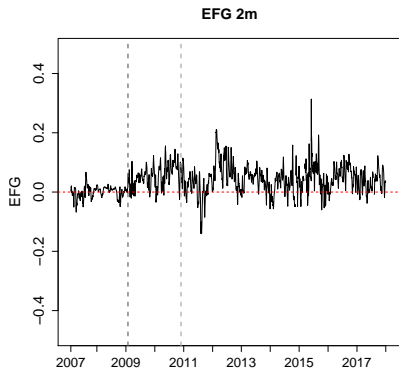
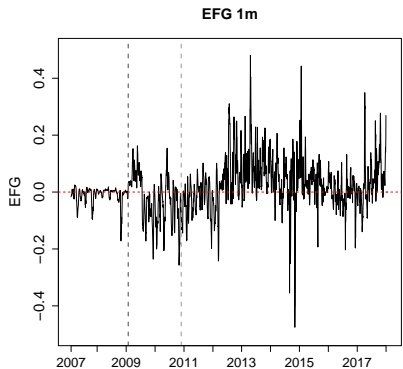
$$(T_2 - T_1)E_t^Q(VIX_{T_1 \rightarrow T_2}^2) = (T_2 - t)E_t^Q(VIX_{t \rightarrow T_2}^2) - (T_1 - t)E_t^Q(VIX_{t \rightarrow T_1}^2)$$



- Second term is a static portfolio of OTM VIX options:

$$\text{Var}_t^Q(VIX_{T_1 \rightarrow T_2}) = 2R_{f,t \rightarrow T_1} \left( \int_{K=0}^{F_{t,T_1}} P_t(K, T_1) dK + \int_{K=F_{t,T_1}}^{\infty} C_t(K, T_1) dK \right)$$

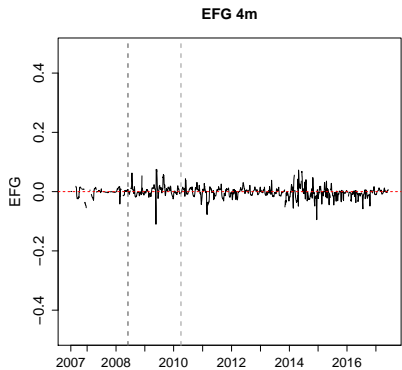
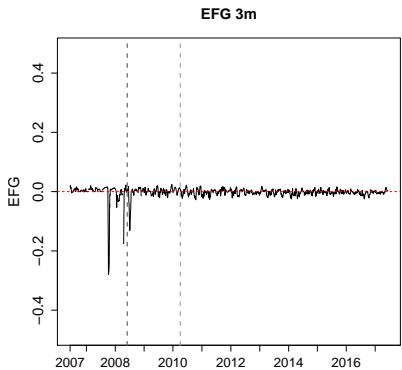
# VIX ETF Futures gap ( $F_{t,T} - E_t^Q(S_T)$ )



1m, 2m

HKM

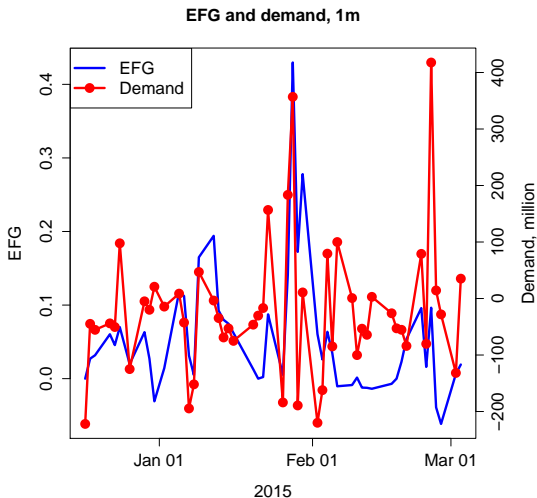
# EFG for other maturities



# VIX ETF Futures gap

- Model-independent. Robust to jumps Derivation for jumps Robust to jumps
- Possible **explanations** for the gap
  - Discretization error in computing  $\text{Var}_t^Q(VIX_{T_1 \rightarrow T_2})$ . But as calls and puts are convex, that would push EFG even higher
  - Liquidity concerns and funding constraints
  - Difference in margin requirements
  - Hedging pressure in the options market
  - Using forward variance swaps instead of options mitigates some of these problems. Produces even higher gap
  - Presence of **ETFs in the VIX futures market**

# EFG ( $F_{t,T} - \mathbb{E}_t^Q(S_T)$ ) and demand of ETFs ( $D_{t,i}^{\$,all}$ )



# Regressions of the EFG ( $F_{t,T} - E_t^Q(S_T)$ )

Dependent variables	EFG <sub>t,1</sub>			EFG <sub>t,2</sub>		
	(1)	(2)	(3)	(4)	(5)	(6)
$D_{t,i}^{\$,all}$	1.21*** (0.25)	<b>0.97**</b> (0.40)		0.57*** (0.15)	<b>0.45***</b> (0.12)	
$D_{t-1,i}^{\$,all}$			<b>0.77***</b> (0.26)			<b>0.38**</b> (0.12)
EFG <sub>t-1,i</sub>		6.03*** (0.72)	6.02*** (0.73)		3.92*** (0.19)	4.09*** (0.22)
Liq <sub>t,i</sub>		0.88** (0.38)	0.75** (0.37)		0.02 (0.11)	0.16 (0.11)
TED <sub>t</sub>		0.51 (0.97)	1.28 (1.06)		1.46*** (0.41)	1.24*** (0.40)
$\alpha_t$		0.62** (0.24)	0.63** (0.25)		-0.33*** (0.12)	0.18 (0.11)
Controls	Yes	Yes	Yes	Yes	Yes	Yes
N	1,898	1,898	1,895	1,824	1,824	1,816
R <sup>2</sup>	0.24	0.44	0.44	0.26	0.58	0.62

Premium. Flow

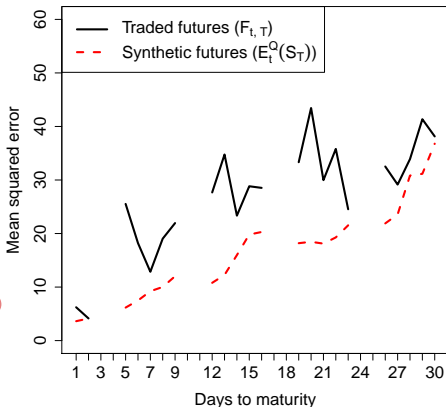
Premium. Level

Returns of futures on EFG



# Mean squared error

- Run predictive regressions of  $S_T$  on  $F_{t,T}$  and  $S_T$  on  $E_t^Q(S_T)$
- $E_t^Q(S_T)$  is a better predictor of the fundamental value  $S_T$  compared to  $F_{t,T}$



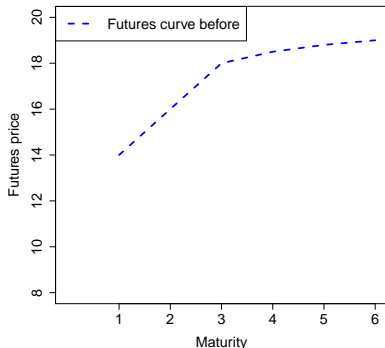
MSE

Time series



# Calendar rebalancing

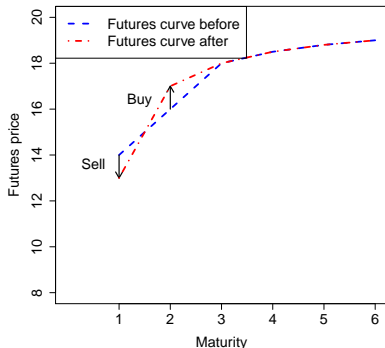
- ETFs roll from the 1st generic futures to the 2nd one. Example:  
Today: 50% in 1st futures, 50% in 2nd futures  
Tomorrow: 45% in 1st futures, 55% in 2nd futures  
...  
In 10 business days: 0% in 1st futures, 100% in 2nd futures



- Analogous to index inclusion/exclusion for equities ETFs

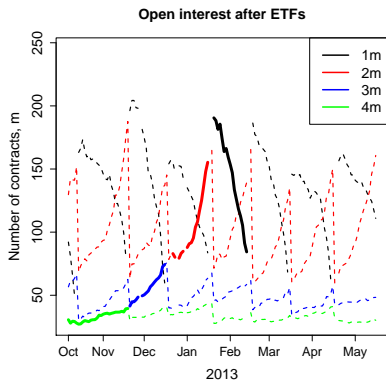
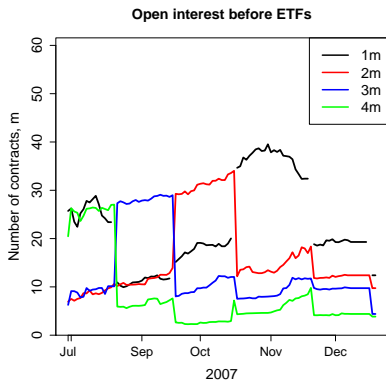
# Calendar rebalancing

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Today: 50% in 1st futures, 50% in 2nd futures  
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- Analogous to index inclusion/exclusion for equities ETFs

# Open interest dynamics before and after ETF introduction



Calendar rebalancing forces early close of futures positions

# Leverage rebalancing

- Some ETFs are leveraged – aim to provide multiples of the daily return of the benchmark  $r_t$ 
  - Leverage  $L > 1$  or  $L < 0$
  - Return every day  $Lr_t$
  - E.g., if  $r_t$  is 10 %, double-long ETF ( $L = 2$ ) should return 20 %
- Always **rebalance in the same direction** as the benchmark return
  - Daily rebalancing demand is  $L(L - 1)AUM_{t-1}r_t$
  - As  $L(L - 1) \geq 0 \forall L \notin [0, 1]$ , both long ( $L > 1$ ) and inverse ( $L < 0$ ) ETFs trade in the same direction as  $r_t$
  - Potential **feedback channel** for prices

Do ETFs actually do that?

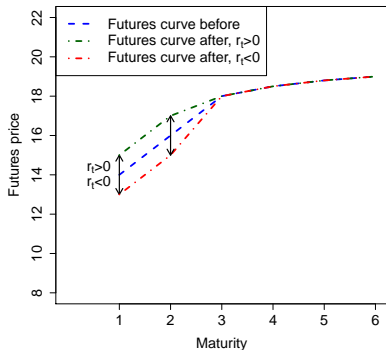
Math derivation

Feedback channel

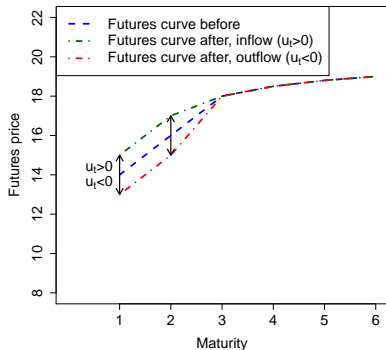
Decomposition

# Leverage rebalancing. Flow rebalancing

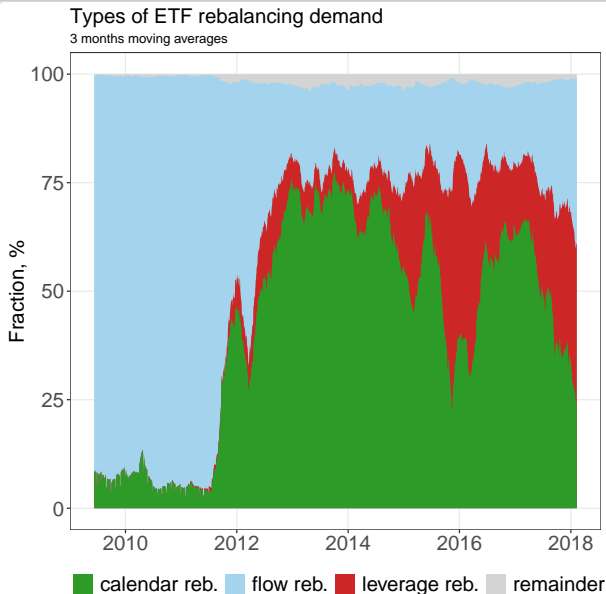
## Leverage rebalancing



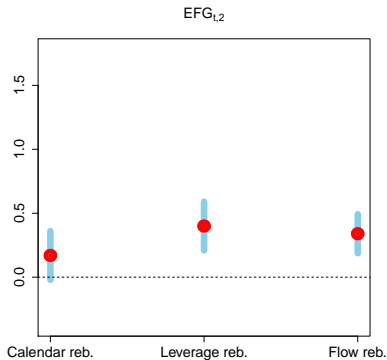
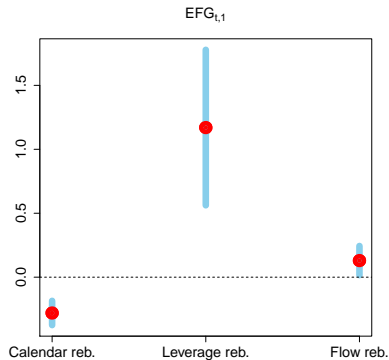
## Flow rebalancing



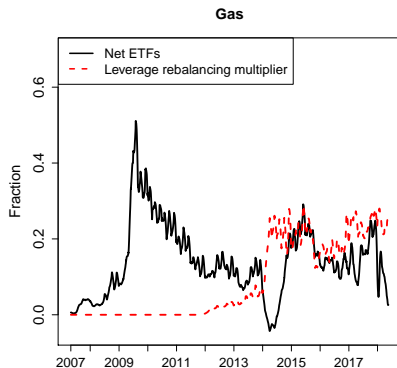
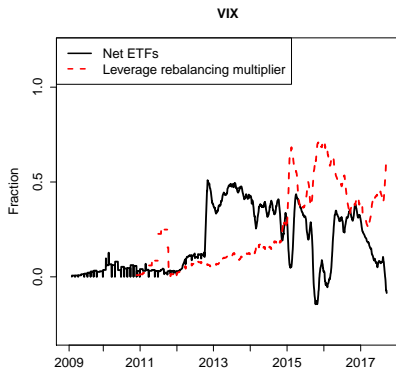
# Demand decomposition. VIX ETFs



# Regressions of EFG on components. VIX



# ETFs' leverage rebalancing



$$\text{Net ETFs} = \frac{\sum_j^N L_j \text{AUM}_j}{\text{Mkt cap}}; L_j - \text{leverage of ETF } j$$

$$\text{Leverage rebalancing multiplier} = \frac{\sum_j^N L_j(L_j - 1) \cdot \text{AUM}_j}{\text{Mkt cap}}$$